[As in previous chapters, there will be substantial rounding in these answers. I have attempted to make the answers fit with the correct values, rather than the exact results of the specific calculations shown here. Thus I may round cell means to two decimals, but calculation is carried out with many more decimals.]

14.1 Does taking the GRE repeatedly lead to higher scores?a. Statistical model:

 $X_{ij} = \mu + \pi_i + \tau_j + \pi \tau_{ij} + e_{ij} \quad \text{or} \quad X_{ij} = \mu + \pi_i + \tau_j + e_{ij}$ 

**b.** Analysis:

Subject	Mean	Test Session	Mean
1	566.67	1	552.50
2	450.00	2	563.75
3	616.67	3	573.75
4	663.33		
5	436.67		
6	696.67		
7	503.33		
8	573.33		
Mean	563.33		

$$SS_{total} = \sum X^{2} - \frac{\left(\sum X\right)^{2}}{N} = 7811200 - \frac{\left(13520\right)^{2}}{24} = 194933.33$$
  
$$SS_{subj} = t\Sigma \left(\bar{X}_{i.} - \bar{X}_{..}\right)^{2}$$
  
$$= 3[\left(566.67 - 563.33\right)^{2} + ... + \left(573.33 - 563.33\right)^{2}] = 3(63222.22) = 189,666.67$$

$$SS_{test} = n\Sigma \left( \bar{X}_{.j} - \bar{X}_{..} \right)^2 = 8[(552.50 - 563.33)^2 + (563.75 - 563.33)^2 + (573.75 - 563.33)^2]$$
  
= 8[226.04] = 1808.33

$$SS_{error} = SS_{total} - SS_{subj} - SS_{test}$$
  
= 194,933.33 - 189,666.67 - 1808.33 = 3458.33

Source	df	SS	MS	F
Subjects	7	189,666.66		
Within subj	16	5266.67		
Test session	2	1808.33	904.17	3.66 ns
Error	14	3458.33	247.02	
Total	23	194,933.33		

### **14.3** Teaching of self-care skills to severely retarded children:

Cell means:			Ph	ase						
		Bas	seline	Tra	ining	Me	an			
Crown	Exp	4.8	4.80		0	5.9	5.90			
Group.	Control	4.7	0	6.4	0	5.5	5			
	Mean	4.7	5	6.7	0	5.7	2			
Subject mea	ans: S	$1 S_2$	$S_3$	$S_4$	$S_5$	S <sub>6</sub>	$S_7$	$S_8$	S <sub>9</sub>	$S_{10}$
Grn Exp	8.	.5 6.0	2.5	6.0	5.5	6.5	6.5	5.5	5.5	6.5
Con Con	trol 4.	0 5.0	9.0	3.5	4.0	8.0	7.5	4.5	5.0	5.5
$\Sigma X^2 = 1501$	$\Sigma X = 22$	29 N	= 40	<i>n</i> =	10	<i>g</i> = 2		<i>p</i> = 2		
$SS_{total} = \sum X^2$	$-\frac{\left(\sum X\right)}{N}$	$\frac{1}{2}$ = 1501 -	$-\frac{229^2}{40} =$	= 189.9	975					
$SS_{subj} = p\Sigma (\overline{X})$	$_{ij.}-\overline{X}_{}\Big)^2$									
=2[(8.5)]	$(-5.72)^{2}$ +	+(5.5-	$-5.72)^2$	]=106	6.475					
$SS_{group} = pn\Sigma($	$\overline{X}_{k} - \overline{X}_{}$	$.)^{2}$								
= 2(8)[	(5.90-5.	$72)^2 + (5.5)^2$	55-5.72	$2)^{2}] =$	1.225					
$SS_{phase} = gn\Sigma \Big($	$\overline{X}_{.j.} - \overline{X}_{}$	$\left( \right)^{2}$								
=2(10)	[(4.75-5	$(5.72)^2 + (6)^2$	5.70-5.2	72) <sup>2</sup> ]=	= 38.02	5				
$SS_{cells} = n\Sigma \left(\overline{X}\right)$	$_{jk}-\overline{X}_{})^2$	2								
=10[(4.	80-5.72	$)^{2} + + (6)^{2}$	5.40-5.	$72)^{2}$	= 39.87	75				
$SS_{PG} = SS_{cells}$ –	- SS <sub>phase</sub> —	$SS_{group} = 3$	9.875 –	38.025	5-1.22	5 = 0.9	25			
Source		df	SS	5	Ν	1S		F		
Between Sub	pi	19	106.47	75						
Groups	5	1	1	.125	1.12	5	0.19	)		
Ss w/in G	rps	18	105	5.250	5.84	7				
Within Subj	-	20	83.500	0						
Phase		1	38	3.025	38.0	25	15.26	6*		
P x G		1	(	).625	0.62	5	0.25	5		
P x Ss w/	in Grps	18	44	4.850	2.49	2				
Total		39	189.97	75						
* p < .05 [F.	$_{05^{(1,18)}}=4.4$	1]								

There is a significant difference between baseline and training, but there are no group differences nor a group x phase interaction.

#### Adding a No Attention control group to the study in Exercise 14.3: 14.5

Total

59

(	Cell means	5:			P	hase					
				Bas	eline	Train	ing	Total			
		Exp		4	.8	7.0	)	5.90			
(	Group	Att Cont	t	4	.7	6.4	ŀ	5.55			
		No Att C	Cont	5	.1	4.6	)	4.85			
		Total		4	.87	6.0	00	5.43			
Subject	means:	$\mathbf{S}_1$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$	$S_8$	<b>S</b> 9	$S_{10}$
Group:	Exp	8.5	6.0	2.5	6.0	5.5	6.5	6.5	5.5	5.5	6.5
	Att	4.0	5.0	9.0	3.5	4.0	8.0	7.5	4.5	5.0	5.0
	Cont										
	No Att	3.5	5.0	7.0	5.5	4.5	6.5	6.5	4.5	2.5	3.0
~	Cont			37	()	10		2			
2	$X^2 = 202$	$26 \Sigma X = X$	\$26326	NN	<del>0</del> 660	$n \equiv 10$	g =\$3=	$^{3}p = 2$	p = 2		
		<i>.</i>	. 2								
22	$-\sum X$	$_{2}$ $(\sum X)$	$\frac{1}{2} - 20$	$326 - \frac{3}{2}$	$326^{2}$ _	254 7333	3				
$SS_t$	otal — <u> </u>	N	- 20	20	60	254.7555	,				
$SS_s$	$u_{bj} = p\Sigma(\bar{X})$	$\overline{K}_{ij.} - \overline{X}_{}$	2								
	=2[(8.5)]	$(5-5.43)^2$	++(3	8.0 - 5.	43) <sup>2</sup> ]=	=159.733					
$SS_{s}$	$g_{group} = pn\Sigma$	$\left(\overline{X}_{k}-\overline{X}\right)$	) <sup>2</sup>								
	=2(8)	[(5.90-5	$(5.43)^2 +$	(5.55-	-5.43)	$^{2} + (4.85)$	-5.43)	<sup>2</sup> ]=11.4	33		
SS	$g_{phase} = gn\Sigma$	$\left(\overline{X}_{.j.}-\overline{X}_{.j.}\right)$	$)^2$								
	=3(10)	)[(4.87-	5.43) <sup>2</sup> -	+(6.00	)-5.43	$(3)^2 = 19.2$	267				
SS	$s_{ells} = n\Sigma \Big(\bar{X}$	$\overline{X}_{.jk} - \overline{X}_{}$	$)^2$								
	=10[(4	4.80-5.4	$(3)^2 + \dots$	+(4.60	)-5.43	$3)^2 = 52.$	333				
SS	$S_{C} = SS_{aclla}$	-SS phase -	- <i>SS</i>	= 51.3	333-19	∕ ∂.267−11	.433=	20.633			
1	-G ceus	phase	group								
S	Source		4	df		SS		M	S	F	
H	Between su	ıbj	29		15	59.7333					
	Groups	-		2		11	.4333	5.71	66	1.04	
	Ss w/ C	Grps		27		14	8.300	5.492	26		
V	Within sub	j	30		ç	95.0000					
	Phase			1		19	.2667	19.2	667	9.44*	
	P * G			2		20	.6333	10.3	165	5.06*	
	P * Ss v	w/Grps		27		55	.1000	2.04	407		

254.733



- **c.** There seems to be no difference between the Experimental and Attention groups, but both show significantly more improvement than the No Attention group.
- **14.7** From Exercise 14.6:
  - **a.** Simple effect of reading ability for children:

$$SS_{RatC} = in\Sigma \left( \bar{X}_{RatC} - \bar{X}_{C} \right)^{2}$$
  
= 3(5)[(4.80 - 3.50)<sup>2</sup> + (2.20 - 3.50)<sup>2</sup>] = 50.70  
$$MS_{RatC} = \frac{SS_{RatC}}{df_{RatC}} = \frac{50.70}{1} = 50.70$$

Because we are using only the data from Children, it would be wise not to use a pooled error term. The following is the relevant printout from SPSS for the Between-subject effect of Reader.

#### Tests of Between-Subjects Effects<sup>a</sup>

Transformed Variable: Average							
Source	Type III Sum of Squares	df	Mean Square	F	Sig.		
Intercept	367.500	1	367.500	84.483	.000		
READERS	50.700	1	50.700	11.655	.009		
Error	34.800	8	4.350				

a. AGE = Children

Measure: MEASURE\_1

**b.** Simple effect of items for adult good readers:

$$SS_{IatAG} = n\Sigma \left( \bar{X}_{IatAG} - \bar{X}_{AG} \right)^2$$
  
= 5[(6.20-5.73)<sup>2</sup> + (6.00-5.73)<sup>2</sup> + (5.00-5.73)<sup>2</sup>] = 4.133

Again, we do not want to pool error terms. The following is the relevant printout from SPSS for Adult Good readers. The difference is not significant, nor would it be for any decrease in the df if we used a correction factor.

Measure: MEASURE_1 Sphericity Assumed						
Source	Type III Sum of Squares	df	Mean Square	F	Sig.	
ITEMS	4.133	2	2.067	3.647	.075	
Error(ITEMS)	4.533	8	.567			

Tests of Within-Subjects Effects

- **14.9** It would certainly affect the covariances because we would force a high level of covariance among items. As the number of responses classified at one level of Item went up, another item would have to go down.
- **14.11** Plot of results in Exercise 14.10:



14.13 Analysis of data in Exercise 14.5 by BMDP:

- **a.** Comparison with results obtained by hand in Exercise 14.5.
- **b.** The *F* for Mean is a test on  $H_0$ :  $\mu = 0$ .
- c.  $MS_{w/in \text{ Cell}}$  is the average of the cell variances.

14.15	Source column of summary table for 4-way ANOVA with repeated measures on A &	: B
	and independent measures on C & D.	

Source
Between Ss
C
D
CD
Ss w/in groups
Within Ss
A
AC
AD
ACD
A x Ss w/in groups
В
BC
BD
BCD
B x Ss w/in groups
AB
ABC
ABD
ABCD
AB x Ss w/in groups
Total

**14.17** Using the mixed models procedure on data from Exercise 14.16

If we assume that sphericity is a reasonable assumption, we could run the analysis with covtype(cs). That will give us the following, and we can see that the F's are the same as they were in our analysis above.

### **Fixed Effects**

Source	Numerator df	Denominator df	F	Sig.
Intercept	1	42.000	450.019	.000
Group	2	42.000	3.749	.032
Time	2	84	73.534	.000
Group * Time	4	84	4.058	.005

Type III Tests of Fixed Effects<sup>a</sup>

a. Dependent Variable: dv.

However, the correlation matrix below would make us concerned about the reasonableness of a sphericity assumption. (This matrix is collapsed over groups, but reflects the separate matrices well.) Therefore we will assume an autoregressive model for our correlations.

Correlations
--------------

		Pre	Post	Followup
Pre	Pearson Correlation	1.000	.585**	.282
Post	Pearson Correlation	.585**	1.000	.616**
Followup	Pearson Correlation	.282	.616**	1.000

\*\*. Correlation is significant at the 0.01 level (2-tailed).

# **Fixed Effects**

#### Type III Tests of Fixed Effects<sup>a</sup>

Source	Numerator df	Denominator df	F	Sig.
Intercept	1	43.256	422.680	.000
Group	2	43.256	3.521	.038
Time	2	81.710	71.356	.000
Group * Time	4	81.710	5.578	.001

a. Dependent Variable: dv.

These *F* values are reasonably close, but certainly not the same.

14.19 Mixed model analysis with unequal size example.

# **Fixed Effects**

Source	Numerator df	Denominator df	F	Sig.
Intercept	1	41.724	393.118	.000
Group	2	41.724	2.877	.068
Time	2	70.480	64.760	.000
Group * Time	4	70.459	5.266	.001

Type III Tests of Fixed Effects<sup>a</sup>

a. Dependent Variable: dv.

Notice that we have a substantial change in the F for Time, though it is still large.

14.21 Everitt's study of anorexia:

**a.** SPSS printout on gain scores:

Tests of	f Between	-Subjects	Effects
----------	-----------	-----------	---------

Dependent Variable: GAIN							
Source	Type III Sum of Squares	df	Mean Square	F	Sig.		
Corrected Model	614.644 <sup>a</sup>	2	307.322	5.422	.006		
Intercept	732.075	1	732.075	12.917	.001		
TREAT	614.644	2	307.322	5.422	.006		
Error	3910.742	69	56.677				
Total	5075.400	72					
Corrected Total	4525.386	71					

a. R Squared = .136 (Adjusted R Squared = .111)

**b.** SPSS printout using pretest and posttest:

#### Tests of Within-Subjects Effects

```
Measure: MEASURE_1
Sphericity Assumed
```

Source	Type III Sum of Squares	df	Mean Square	F	Sig.			
TIME	366.037	1	366.037	12.917	.001			
TIME * TREAT	307.322	2	153.661	5.422	.006			
Error(TIME)	1955.371	69	28.339					

c. The F comparing groups on gain scores is exactly the same as the F for the interaction in the repeated measures design.





The plots show that there is quite a different relationship between the variables in the different groups.

### e. Treatment Group = Control

One-Sample Statistics <sup>a</sup>						
	Ν	Mean	Std. Deviation	Std. Error Mean		
GAIN	26	4500	7.9887	1.5667		

a. Treatment Group = Control

#### One-Sample Test<sup>a</sup>

	Test Value = 0						
				Mean	95% Confider of the Di	nce Interval fference	
	t	df	Sig. (2-tailed)	Difference	Lower	Upper	
GAIN	287	25	.776	4500	-3.6767	2.7767	

a. Treatment Group = Control

This group did not gain significantly over the course of the study. This suggests that any gain we see in the other groups cannot be attributed to normal gains seen as a function of age.

- **f.** Without the control group we could not separate gains due to therapy from gains due to maturation.
- 14.23 t = -0.555. There is no difference in Time 1 scores between those who did, and did not, have a score at Time 2.
  - **b**. If there had been differences, I would worried that people did not drop out at random. to answer.

14.25	Differences	due	to	Judges	play	an	important	role.
-------	-------------	-----	----	--------	------	----	-----------	-------

14.27 If I were particularly interested in differences between subjects, and recognized that judges probably didn't have a good anchoring point, and if this lack was not meaningful, I would not be interested in considering it.

### 14.29 Strayer et al. (2006)

#### Tests of Between-Subjects Effects

Measure:MEASURE\_1 Transformed Variable:Average

Source	Type III Sum of Squares	df	Mean Square	F	Siq.
Intercept	7.711E7	1	7.711E7	724.691	.000
Error	4149966.533	39	106409.398		

#### **Tests of Within-Subjects Effects**

Measure:MEASUR	Measure:MEASURE 1								
Source		Type III Sum of Squares	df	Mean Square	F	Siq.			
Condition	Sphericity Assumed	134696.067	2	67348.033	4.131	.020			
	Greenhouse-Geisser	134696.067	1.992	67619.134	4.131	.020			
	Huynh-Feldt	134696.067	2.000	67348.033	4.131	.020			
	Lower-bound	134696.067	1.000	134696.067	4.131	.049			
Error(Condition)	Sphericity Assumed	1271689.267	78	16303.709					
	Greenhouse-Geisser	1271689.267	77.687	16369.337					
	Huynh-Feldt	1271689.267	78.000	16303.709					
	Lower-bound	1271689.267	39.000	32607.417					

#### **b.** Contrasts on means:

Because the variances within each condition are so similar, I have used  $MS_{error(within)}$  as my error term. The means are 776.95, 778.95, and 849.00 for Baseline, Alcohol, and Cell phone conditions, respectively..

$$t = \frac{\hat{\psi}}{\sqrt{\frac{\sum a_i^2 MS_{error}}{n}}}}$$

$$\hat{\psi}_{1vs2} = 776.95 - 778.95 = 2$$

$$\hat{\psi}_{1vs3} = 776.95 - 849.00 = 72.05$$

$$\hat{\psi}_{2vs3} = 778.95 - 849.00 = 70.5$$

$$den = \sqrt{\frac{\sum a_i^2 MS_{error}}{n}} = \sqrt{\frac{2 \times 16303.709}{40}} = 28.551$$

$$t_{1vs2} = 2/28.551 = 0.07$$

$$t_{1vs3} = 72.05/28.551 = 2.52^*$$

$$t_{2vs3} = 70.05/28.551 = 2.45^*$$

Both Baseline and Alcohol conditions show poorer performance than the cell phone condition, but, interestingly, the Baseline and Alcohol conditions do not differ from each other.