# 8. Comparing Means Using One Way ANOVA

## Objectives

- ♦ Calculate a one-way analysis of variance
- ♦ Run various multiple comparisons
- ♦ Calculate measures of effect size

A One Way ANOVA is an analysis of variance in which there is only one independent variable. It can be used to compare mean differences in 2 or more groups. In SPSS, you can calculate one-way ANOVAS in two different ways. One way is through Analyze/Compare Means/One-Way ANOVA and the other is through Analyze/General Linear Model/Univariate. We'll try both in this chapter so we can compare them.

## **One-Way ANOVA**

Let's begin with an example in the textbook illustrated in Table 16.6. Maternal role adaptation was compared in a group of mothers of low birth-weight (LBW) infants who had been in an experimental intervention, mothers of LBW infants who were in a control group, and mothers of full-term infants. The hypothesis was that mothers of LBW infants in the experimental intervention would adapt to their maternal role as well as mothers of healthy full-term infants, and each of these groups would adapt better than mothers of LBW infants in the control group.

✓ **Open** *maternal role adaptation.sav*.

### ✓ Select Analyze/Compare Means/One-Way ANOVA.

✓ Select maternal role adaptation for the Dependent List since it is the dependent variable. Select group as the Factor or independent variable. Then click Post Hoc to see various options for calculating multiple comparisons. If the ANOVA is significant, we can use the post hoc tests to determine which specific groups differ significantly from one another.



Cone-Way ANOVA: Post Hoc Multiple Comparisons						
FEqual Variances A	ssumed					
	<u>s</u> -N-K	<u>W</u> aller-Duncan				
Bonferroni	<u>T</u> ukey	Type I/Type II Error Ratio: 100				
Sidak	Tu <u>k</u> ey's-b	Dunnett				
Scheffe	Duncan	Control Category : Last				
R-E-G-W F	<u>H</u> ochberg's GT2	Test				
🗌 R-E-G-W <u>Q</u>	<u>G</u> abriel	$\bigcirc$ <u>2</u> -sided $\bigcirc$ < Control $\bigcirc$ > Control				
Equal Variances N	lot Assumed					
Ta <u>m</u> hane's T2	Dunnett's T <u>3</u>	Games-Howell Dunnett's C				
Significance level: 0.05						
Continue Cancel Help						

 ✓ As you can see, there are many options. Let's select
 LSD under Equal Variances
 Assumed since it is Fisher's
 Least Significant Difference
 Test which is calculated in the text, except that SPSS will test the differences even if the overall *F* is not significant.

- ✓ Note that .05 is the default under Significance level. After consulting with SPSS technical support, it is clear that this is the experiment-wise or family-wise significance level. So any comparison flagged by SPSS as significant is based on a Bonferroni Type Correction. You do not need to adjust the significance level yourself.
- Click Options. In the next dialog box, select
   Descriptives under Statistics, and select Means plot so SPSS will create a graph of the group means for us. The default under Missing Values is Exclude cases analysis by analysis. Let's leave this as is. Click
   Continue and then Ok. The output follows.

Adapt

🚰 Independent-Samples T Test: Options 🗵					
<u>C</u> onfidence Interval: 95 %					
Missing Values					
Exclude c <u>a</u> ses analysis by analysis					
O Exclude cases listwise					
Continue Cancel Help					

#### Descriptives

					95% Confidence Interval for Mean			
	N	Mean	Std. Deviation	Std. Error	Lower Bound	Upper Bound	Minimum	Maximum
LBW-Exp	29	14.97	4.844	.899	13.12	16.81	10	29
LBW-Control	27	18.33	5.166	.994	16.29	20.38	10	29
Full-Term	37	14.84	3.708	.610	13.60	16.07	10	25
Total	93	15.89	4.747	.492	14.91	16.87	10	29

#### ANOVA

Adapt								
	Sum of Squares	df	Mean Square	F	Sig.			
Between Groups	226.932	2	113.466	5.532	.005			
Within Groups	1845.993	90	20.511					
Total	2072.925	92						

# **Post Hoc Tests**

#### **Multiple Comparisons**

Adapt LSD

					95% Confidence Interval	
(I) Group	(I) Group	Mean Difference (I- .I)	Std Error	Sia	Lower Bound	Upper Bound
LBW-Exp	LBW-Control	-3.368	1.211	.007	-5.77	96
	Full-Term	.128	1.123	.910	-2.10	2.36
LBW-Control	LBW-Exp	3.368*	1.211	.007	.96	5.77
	Full-Term	3.495 <sup>*</sup>	1.146	.003	1.22	5.77
Full-Term	LBW-Exp	128	1.123	.910	-2.36	2.10
	LBW-Control	-3.495	1.146	.003	-5.77	-1.22

\*. The mean difference is significant at the 0.05 level.

## **Means Plots**



GROUP

✓ Compare this output to the results presented in the text.

We can see the descriptive statistics and the F value are the same. It is harder to compare the post hoc comparisons because SPSS does not display the t values. They simply report the mean difference and the significance level. The important thing to note is that the conclusions we can draw based on each of these approaches are the same.

The plot that SPSS created is an effective way to illustrate the mean differences. You may want to edit the graph using what you learned in Chapter 3 to make it more elegant. Some people would prefer a bar chart since these are independent groups and a line suggests they are related. You could create a bar chart of these group means yourself.

Let's re-run the same analysis using the General Linear Model (GLM) and see how they are similar and different.

## General Linear Model to Calculate One-Way ANOVAs

The Univariate General Linear Model is really intended to test models in which there is one dependent variable and multiple independent variables. We can use it to run a simple one-way ANOVA like the one above. One advantage of doing so is that we can estimate effect size from this menu, but we could not from the One-Way ANOVA menus. Let's try it.

## ✓ Select Analyze/General Linear Model/Univariate.



- ✓ As you can see by this dialog box, there are many more options than the One-Way ANOVA. This is because the GLM is a powerful technique that can examine complex designs. We'll just focus on what is relevant to us. As before, select maternal role adaptation as the Dependent Variable and group as the Fixed Factor or independent variable. Then, click Plots.
- Select group for the Horizontal Axis (X axis), and click add. Since there is only one dependent variable, SPSS knows that maternal role adaptation is on the Y axis without us needing the specify this. Click Continue.

Eactors: Group		• •	Horizontal Axis: Separate Lines: Segarate Plots:
Plo <u>t</u> s: Group	Add	<u>C</u> har	nge <u>R</u> emove
	Continue	Cancel	Help

🚰 Univariate: P	ost Hoc Multiple C	omparisons for Observed Means 🛛 🗙
Eactor(s):		Post Hoc Tests for:
Group		Group
Fequal Varianc	es Assumed	
	<u>s-N-K</u>	<u>Waller-Duncan</u>
Bonferroni	<u>T</u> ukey	Type I/Type II Error Ratio: 100
Sidak	Tukey's-b	Dunnett
Scheffe	Duncan	Control Category; Last 💌
<u>R</u> -E-G-VV-F	Hochberg's GT2	Test
R-E-G-W-Q	Gabriel	
Equal Variance	es Not Assumed 2 Dunnett's T <u>3</u>	Games-Howell Dunnett's C
	Continue	Cancel Help

✓ Since this procedure can be used with multiple independent variables, we need to specify which ones to run post hoc comparisons for even though there is only one in our design. Select group for **Post Hoc Tests for**. This time, let's select **Bonferroni** to see if it makes a difference.

✓ Under Display, select Descriptive statistics and Estimates of effect size. Then click Continue. In the main dialog box, click Ok. The output follows.

🚰 Univariate: Options	X
Estimated Marginal Means Eactor(s) and Factor Interactions: (OVERALL) Group	Display <u>M</u> eans for: Group
	Confidence interval adjustment: LSD(none)
Display	
Descriptive statistics	<u>H</u> omogeneity tests
✓ Estimates of effect size	Spread vs. level plot
Observed power	<u>R</u> esidual plot
Parameter estimates	Lack of fit
Contrast coefficient matrix	<u>G</u> eneral estimable function
Significance le <u>v</u> el: .05 Confiden	ice intervals are 95.0%
Continue	Cancel Help

#### **Between-Subjects Factors**

		Value Label	N
Group	1	LBW-Exp	29
	2	LBW-Control	27
	3	Full-Term	37

## **Descriptive Statistics**

Group	Mean	Std. Deviation	N
LBW-Exp	14.97	4.844	29
LBW-Control	18.33	5.166	27
Full-Term	14.84	3.708	37
Total	15.89	4.747	93

#### Tests of Between-Subjects Effects

Dependent Variable:Adapt								
Source	Type III Sum of Squares	df	Mean Square	F	Sig.	Partial Eta Squared		
Corrected Model	226.932ª	2	113.466	5.532	.005	.109		
Intercept	23513.095	1	23513.095	1146.364	.000	.927		
Group	226.932	2	113.466	5.532	.005	.109		
Error	1845.993	90	20.511					
Total	25562.000	93						
Corrected Total	2072.925	92						

a. R Squared = .109 (Adjusted R Squared = .090)

# **Post Hoc Tests** Group

#### **Multiple Comparisons**

Adapt Bonferroni						
					95% Confide	ence Interval
	( ) 0	Mean Difference (l-	Otal Cases	0in	Lauran Darrind	Line on Down d
(I) Group	(J) Group	J)	Sta. Error	Siq.	Lower Bound	Opper Bound
LBW-Exp	LBW-Control	-3.37*	1.211	.020	-6.32	41
	Full-Term	.13	1.123	1.000	-2.61	2.87
LBW-Control	LBW-Exp	3.37*	1.211	.020	.41	6.32
	Full-Term	3.50 <sup>*</sup>	1.146	.009	.70	6.29
Full-Term	LBW-Exp	13	1.123	1.000	-2.87	2.61
	LBW-Control	-3.50*	1.146	.009	-6.29	70

Based on observed means. The error term is Mean Square(Error) = 20.511.

\*. The mean difference is significant at the .05 level.

## **Profile Plots**



 Compare this output to the output from the One-Way ANOVA and the results in the textbook.

One difference is the appearance of the ANOVA summary table. Now, there is a row labeled intercept and another labeled adjusted. You can ignore these. The *F* value for Group is still the same, and that is what we are interested in. Notice the eta squared column. What does it say for group? Does this value agree with the text? Unfortunately SPSS does not calculate Omega squared, so you would have to do this by hand. (Unfortunately, it also does not calculate any of the more useful effect size measures, such as d. Did the Bonferroni and the previous LSD multiple comparisons yield the same results?

You could edit any of the tables and graphs to look more elegant. For example, the current title of the graph is cut off. You would probably want to name it something else or use two lines of text. Editing the output would be ideal if you wanted to include your output in a paper. Use what you learned in Chapters 3 and 4 of this Manual to do so.

In this chapter, you learned 3 methods to calculate a One-Way ANOVA. I prefer the General Linear Model approach since this is the only one that gives us the option of calculating multiple comparisons and eta squared. Of course, you may feel otherwise depending on the information you wish to calculate. Complete the following exercises.

## Exercises

Each of these exercises is based on *Eysenck recall.sav*. This study is presented in section 16.1 in the textbook.

- 1. Use ANOVA to compare the means. Select a post hoc procedure of your choice. Summarize the results.
- 2. Edit the ANOVA summary table so that it is suitable for inclusion in a paper.

- 3. Use SPSS to calculate eta squared. Note, how did you do this?
- 4. Create a bar chart to illustrate the differences between groups.