

1. We are interested in testing the following hypotheses about the average weight of students at a college:

$$H_0 : \mu = 68$$

$$H_1 : \mu > 68$$

A SRS of  $n=36$  students will be used and we will assume that  $\sigma$  is known to be 6 kg.

- Find  $\alpha$  if we choose to reject  $H_0$  if we observe a sample with  $\bar{y} > 69$ .
  - Find  $\beta$  if the true mean weight is 70.5 kg.
  - Find the power to detect a true mean of 69.8 kg.
  - Answer part (c) if we use a larger sample of  $n=64$  students.
2. Blood pressure for American women aged 18-44 is approximately normal with a mean of 75 mm Hg and a standard deviation of 10 mm Hg. A sample of  $n=25$  women who jog at least 5 miles/week has a sample average blood pressure of 70.9 mm Hg.

The research question is: Does the data provide strong evidence that the mean blood pressure for those who exercise regularly is not equal to 75 mm Hg?

- State the hypotheses ( $H_0$  and  $H_a$ ) to be tested and find the p-value for these data.
  - Write the rejection region (RR) in terms of z-scores and test  $H_0$  at the  $\alpha = .03$  level.
  - Write the RR for  $H_0$  in terms of  $\bar{X}$ .
  - Find the probability of a Type II error if the true mean is 73 mm Hg.
3. Let  $Y$  be a random variable denoting the number of pips showing on a die that is tossed
- Find  $E(Y)$
  - Find  $\text{Var}(Y)$
  - Find  $E(3Y + 2)$
  - Find  $\text{Var}(3Y + 2)$
4. Suppose that  $X$  is a random variable with  $E(X+4)=10$  and  $E[(X+4)^2]=116$
- Find  $\text{Var}(X+4)$
  - Find  $\mu$
  - Find  $\sigma^2$