

$$(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^k y^{n-k}$$

### **Binomial Random Variable (Independent Trials Model)**

- $n$  independent Bernoulli trials [with a Success or Failure ( $S$  or  $F$ ) on each]
- $P(\text{Success}) = p$  for each trial
- $\mathbf{X}$  = # of Successes in  $n$  independent trials  $\rightarrow \mathbf{X} \sim \text{Binomial}(n, p)$
- PMF:  $f(x) = P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$
- If  $X_1, X_2, \dots, X_n$  are indep. Bernoulli( $p$ ) RVs (a Random Sample of size  $n$  from the distribution)  
Then  $\mathbf{X} = X_1 + X_2 + \dots + X_n$  is a Binomial( $n, p$ ) RV

$\mathbf{X}$  = # of pips on a die

$F(x) = P(X \leq x)$

