

1. Linear Motion; Constant Acceleration:

$$v = v_0 + at$$

$$x = x_0 + v_0 t + \frac{1}{2} at^2$$

$$x = \frac{1}{2} (v_0 + v) t$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

2. Forces:

$$\Sigma \mathbf{F} = m\mathbf{a}$$

$$f_s^{MAX} = \mu_s n$$

$$f_k = \mu_k n$$

3. Work; Energy; Power:

$$W = F_{\parallel} s = (F \cos \theta) s$$

$$K_{trans} = \frac{1}{2} mv^2$$

$$U_{grav} = mgy$$

Linear ($F = -kx$) spring:

$$U_{spring} = \frac{1}{2} kx^2$$

$$\bar{P} = W/\Delta t = F\bar{v}$$

4. Linear Momentum:

$$\mathbf{p} = m\mathbf{v}$$

$$\Sigma \mathbf{F} = \Delta \mathbf{p} / \Delta t$$

5. Gravitation

$$F_G = Gm_1 m_2 / R^2$$

$$U_G = -Gm_1 m_2 / R$$

where $G = 6.672 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$

At earth's surface:

$$F_G = mg \text{ where } g = 9.8 \text{ m/s}^2.$$

Satellite Motion: $T^2 = (4\pi^2 / MG) R^3$

Sun: $M_S = 2 \times 10^{30} \text{ kg}$

Earth: $M_E = 6 \times 10^{24} \text{ kg}$
 $R_E = 6.37 \times 10^6 \text{ m}$
 from sun $= 1.5 \times 10^{11} \text{ m}$

Moon: $M_M = 7.4 \times 10^{22} \text{ kg}$
 $R_M = 1.74 \times 10^6 \text{ m}$
 from earth $= 3.8 \times 10^8 \text{ m}$

6. Rotational Motion:

$$\omega = \omega_0 + \alpha t$$

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\theta = \frac{1}{2} (\omega_0 + \omega) t$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

$$s = r\theta$$

$$v_t = r\omega$$

$$a_T = r\alpha$$

$$a_C = v_t^2 / r = r\omega^2$$

$$L = I\omega$$

$$K_{rot} = \frac{1}{2} I\omega^2$$

$$\tau = R_{\perp} F = RF_{\perp} = RF \sin \theta$$

$$\Sigma \tau = I\alpha = \Delta L / \Delta t$$

7. Rotational Inertia:

$$I = \Sigma_i m_i R_i^2$$

solid cylinder: $I_{CM} = \frac{1}{2} MR^2$

hoop: $I_{CM} = MR^2$

sphere: $I_{CM} = \frac{2}{5} MR^2$

rod ($\perp$ to length): $I_{CM} = \frac{1}{12} ML^2$

rod (through end): $I_{END} = \frac{1}{3} ML^2$

8. Vibrations:

For Simple Harmonic Motion:

$$x = A \cos \omega t$$

$$v = -\omega A \sin \omega t$$

$$a = -\omega^2 A \cos \omega t = -\omega^2 x$$

where $\omega = 2\pi f$

and $f = 1/T$

$$E = \frac{1}{2} kA^2$$

For a mass/spring

$$\omega = \sqrt{k/m}$$

For a Simple Pendulum

$$\omega = \sqrt{g/L}$$

9. Waves & Sound

Wave velocity:

$$v = \lambda f$$

Intensity:

$$I = P/A$$

$$I = P/4\pi r^2$$

$$v_{air} = 343 \text{ m/s (at } 20^\circ \text{C)}$$

$$v_{string} = \sqrt{F/\mu}$$

$$\mu = m/L$$

$$\beta(\text{dB}) = 10 \log(I/I_0)$$

$$\text{where } I_0 = 10^{-12} \text{ W/m}^2$$

Doppler:

$$f' = \left(\frac{v \pm u_o}{v \mp u_s} \right) f$$

Organ Pipes:

$$f_n = n(v/2L), \quad \lambda_n = 2L/n$$

where $n = 1, 2, 3, \dots$ (ends open)

$$f_n = n(v/4L), \quad \lambda_n = 4L/n$$

where $n = 1, 3, 5, \dots$ (one end closed)

Vibrating strings have a mode structure like open pipes.

$$\text{Beats: } f_{beat} = |f_1 - f_2|$$