Exam I

Math 021 Section Z1 Instructor: Eric Clark June 2, 2014

- $\bullet\,$ The exam is out of 60 points. There are a total of 6 questions, 10 points each.
- Do not discuss the contents of this exam with anyone. (including Google!)
- You must show all work to receive full credit.

Name_____

Problem 1: Continuity.

a: Using interval notation, give the interval where the function is continuous:

$$f(x) = \frac{\ln(x^2 - 4)}{x^2 - 16}$$

b: Find the value of k that makes the function continuous: $f(x) = \begin{cases} kx^2 + 1 & \text{if } x \leq 2 \\ x + k & \text{if } x > 2 \end{cases}$

Problem 2: Evaluate the following limits.

a:
$$\lim_{x \to -2} \frac{x^3 - 3x^2 - 10x}{x^2 + 2x}$$

b)
$$\lim_{x \to 81} \frac{\sqrt{x} - 9}{x - 81}$$

c:
$$\lim_{x \to \infty} \frac{8 - 4x^3}{5x^2 + 7x + 10}$$

d:
$$\lim_{x \to \infty} \frac{\sqrt{5x + 3x^4}}{6 + 7x + 4x^2}$$

Problem 3: Suppose the position function of a skier during a run can be modeled by the function: $s(t) = 3x^2 + 4x$. Where t is time measured in seconds, the position s(t) is measured in meters from the base lodge.

a) Find the velocity function, v(t) = s'(t), using the formal definition of the derivative

$$s'(x) = \lim_{h \to 0} \frac{s(x+h) - s(x)}{h}$$

b) Find the average velocity between $t_1 = 1$ and $t_2 = 3$ seconds. (Hint: This is an average rate of change, or the slope of the secant line between these two points : $s_{avg} = \frac{s(t_2) - s(t_1)}{t_2 - t_1}$

Problem 4: For each of the following functions find the derivative with respect to x.

a) a:
$$\frac{d}{dx}[x^5 + 3\pi^2 x^3 + \ln(6)]$$

b)
$$\frac{d}{dx}\left[\frac{x^2+\sqrt{x}}{x}\right] =$$

c)
$$\frac{d}{dx}[3x^{\frac{1}{3}} + 2\sqrt{x} - \frac{1}{x}] =$$

d) Let $f(x) = x^3 + 4x^2 + 5$. Find f'(x). Then find the equation of the tangent line when x = 1 i.e. at the point (1,f(1))

Problem 5: For each of the following functions find the derivative with respect to x. **a:** $f(x) = (\sqrt{x^3 + 1})(x + 5)^5$

b:
$$f(x) = \frac{\ln(x^2)}{x^2 + 1}$$

c:
$$f(x) = e^{x^3}(x^2 + 1)$$

Problem 6: For each of the following functions find the derivative with respect to x.

a)
$$f(x) = (2x^5 + 3x^3 + 3x + 5)^{10}$$

b) $g(x) = e^{(3x^2 + \sqrt{x})^3}$

c)
$$f(x) = \ln(4x^2 + 3)^{4/5}$$