Name:

Problem 1: Let X be a topological space with topology \mathcal{T} , and let Y be a subset of X. Give the definition of the subspace topology on Y.

Solution: The subspace topology on Y contains exactly the following open sets:

$$\{Y \cap U \mid U \in \mathcal{T}\}.$$