

1. Give an example of a 2×2 (two equations in two unknowns) system of linear equations such that
 - (a) The system has a unique solution.
 - (b) The system has no solution.
 - (c) The system has infinitely many solutions.
2. Solve the following system of linear equations.

$$3x_1 - x_2 + 2x_3 + 4x_4 + x_5 = 2$$

$$x_1 - x_2 + 2x_3 + 3x_4 + x_5 = -1$$

$$2x_1 - 3x_2 + 6x_3 + 9x_4 + 4x_5 = -5$$

$$7x_1 - 2x_2 + 4x_3 + 8x_4 + x_5 = 6$$

3.
 - (a) Solve problem 3.18 in Section One.I.3. You should get two general solutions that look different.
 - (b) The vector $\begin{pmatrix} 0 \\ 0 \\ 4 \end{pmatrix}$ is a solution of this system. In the **first** of your general solutions, what value of the parameter gives you this solution?
 - (c) The vector $\begin{pmatrix} 0 \\ 0 \\ 4 \end{pmatrix}$ is a solution of this system. In the **second** of your general solutions, what value of the parameter gives you this solution?
 - (d) The vector $\begin{pmatrix} -5 \\ 1 \\ 10 \end{pmatrix}$ is a solution of this system. In the **first** of your general solutions, what value of the parameter gives you this solution?
 - (e) The vector $\begin{pmatrix} -5 \\ 1 \\ 10 \end{pmatrix}$ is a solution of this system. In the **second** of your general solutions, what value of the parameter gives you this solution?
 - (f) Plug in the value 2 for the parameter into each of your two general solutions. Do you get the same particular solution? Is that okay?