

Name:

**Problem 1:** Suppose that there exists a relation between two variables  $u$  and  $v$ . The ordered pairs belonging to this relation are presented in the table below:

$u$		2		5		3		-2		2
$v$		3		-3		1		0		6

Circle the **one** correct statement describing this situation:

- a)  $u$  is **not** a function of  $v$  and  $v$  is **not** a function of  $u$
- b)  $u$  **is** a function of  $v$ , but  $v$  is **not** a function of  $u$
- c)  $u$  is **not** a function of  $v$ , but  $v$  **is** a function of  $u$
- d)  $u$  **is** a function of  $v$  and  $v$  **is** a function of  $u$

You do not need to show any work if you do not want to.

**Solution:** We first note that  $u$  cannot be the independent variable of a function, since the two pairs  $(u = 2, v = 3)$  and  $(u = 2, v = 6)$  are part of the relation. Therefore the input  $u = 2$  does not have a single, well-defined output. Therefore,  $v$  is **not** a function of  $u$ .

We now consider  $v$  as the possible independent variable. We note that each value of  $v$  given is different. Therefore it must be the case that each input  $v$  corresponds to a single, well-defined output  $u$ . (Since each value of  $v$  appears only once, it can only be assigned one output.) Therefore,  $u$  **is** a function of  $v$ .

The answer is b).