Exercise 1

Given any $g, r \geq 3$, does there exist a an r-regular bipartite graph of girth at least g?

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Exercise 2

Find the maximum number of edges in a graph on n vertices that does not have two vertex-disjoint triangles.

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Exercise 3 (3.21)

Suppose x is not a cut vertex and its degree is at least 2k. Prove that there are at least k edge-disjoint cycles containing x.

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