

1. Forces:

$$\Sigma \vec{F} = m\vec{a}$$

$$\Sigma F_x = ma_x$$

$$\Sigma F_y = ma_y$$

$$F = mg$$

$$f_{s\ max} = \mu_s n$$

$$f_k = \mu_k n$$

$$F = -k\Delta x$$

2. Rotational Dynamics:

$$L = I\omega$$

$$K_{rot} = \frac{1}{2} I\omega^2$$

$$\tau = r_{\perp} F = rF_{\perp} = rF \sin \phi$$

$$\Sigma \tau = I\alpha = \Delta L / \Delta t$$

3. Rotational Inertia:

$$I = \Sigma_i m_i R_i^2$$

$$\text{solid cylinder: } I_{CM} = \frac{1}{2} MR^2$$

$$\text{hoop: } I_{CM} = MR^2$$

$$\text{solid sphere: } I_{CM} = \frac{2}{5} MR^2$$

$$\text{hollow sphere: } I_{CM} = \frac{2}{3} MR^2$$

$$\text{rod } (\perp \text{ to length}): I_{CM} = \frac{1}{12} ML^2$$

$$\text{rod (through end): } I_{END} = \frac{1}{3} ML^2$$

4. Impulse & Momentum:

$$(\Sigma \vec{F}) \Delta t = m\vec{v}_f - m\vec{v}_i$$

$$m_1 \vec{v}_{f1} + m_2 \vec{v}_{f2} = m_1 \vec{v}_{i1} + m_2 \vec{v}_{i2}$$

$$v_{cm} = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$

$$v_{f1} = \frac{m_1 - m_2}{m_1 + m_2} v_{i1}, \quad v_{f2} = \frac{2m_1}{m_1 + m_2} v_{i1}$$

5. Work; Energy; Power:

$$W = (F \cos \theta) d$$

$$K = \frac{1}{2} mv^2$$

$$U_g = mgy$$

Linear ($F = -kx$) spring:

$$U_s = \frac{1}{2} kx^2$$

$$E = K + U_g + U_s + E_{th} + E_{chem} + \dots$$

$$\Delta E = \Delta K + \Delta U_g + \Delta U_s + \Delta E_{th} + \Delta E_{chem} + \dots = W$$

$$P = \Delta E / \Delta t = W / \Delta t = Fv$$

6. Using Energy:

$$e = \frac{\text{What you get}}{\text{What you have to pay}} = COP$$

1st Law of Thermodynamics:

$$\Delta E_{th} = Q + W$$

2nd Law of Thermodynamics:

The entropy of an isolated system always increases

$$e_{max} = 1 - \frac{T_C}{T_H}$$

$$COP_{max, cooling} = \frac{T_C}{T_H - T_C}$$

$$COP_{max, heating} = \frac{T_H}{T_H - T_C}$$

7. Heat & Temperature

Temperature Scales:

$$T_C = \frac{5}{9} (T_F - 32.0)$$

$$T_F = \frac{9}{5} T_C + 32.0$$

$$T_K = T_C + 273.15$$

Heat Capacity: $Q = Mc\Delta T$

Latent Heat of Transformation:

$$Q = \pm ML_f \text{ or } Q = \pm ML_v$$

Molar specific Heat (of an ideal Gas):

$$Q = nC_V \Delta T \text{ or } Q = nC_P \Delta T$$

8. Ideal Gases & Kinetic Theory

Mole, Mass, Avogadro's Number:

$$n = N / N_A$$

$$n = m / (\text{mass per mole})$$

$$m_{particle} = (\text{mass per mole}) / N_A$$

Ideal Gas Law:

$$pV = nRT = Nk_B T$$

Kinetic Theory of Gases:

$$K_{avg} = \frac{1}{2} m v_{rms}^2 = \frac{3}{2} k_B T$$

$$v_{rms} = \sqrt{\frac{3k_B T}{m}}$$

$$E_{th} = \frac{3}{2} nRT$$

9. Constants:

$$N_A = 6.02 \times 10^{23}$$

$$R = 8.31 \text{ J}/(\text{mol} \cdot \text{K})$$

$$k_B = R / N_A = 1.38 \times 10^{-23} \text{ J/K}$$

$$g = 9.80 \text{ m/s}^2$$