

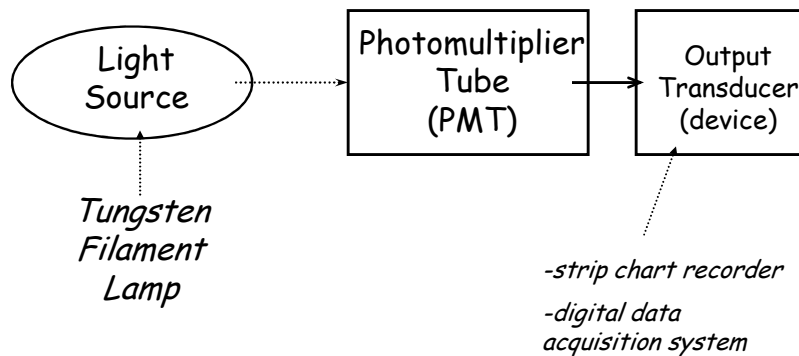
January 25, 2012

- Textbook will be placed on reserve in Library
- Solutions to Prob Set #1 have been posted

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Hypothetical Instrument

- Let's explore the signal and noise behavior of a simple light measurement instrument:



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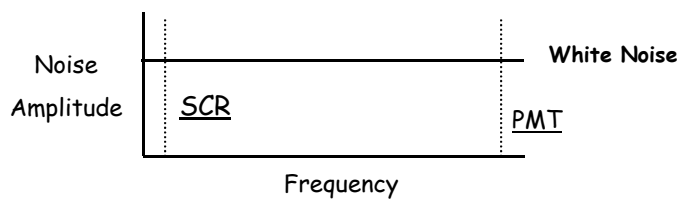
Reducing Δf

- Look at *frequency response* of instrument components:

PMT: 10^7 Hz

SCR: 10^0 Hz

DDA: $10^0 - 10^7$ Hz (variable)



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S/N Enhancement: Impact of Δf

- Output device/transducer limits Δf :

$$\frac{S/N(\Delta f = 10^0)}{S/N(\Delta f = 10^7)} \approx 10^3$$

- Δf can be easily adjusted using a *low-pass* frequency filter
- BUT: remember that Δf also affects ability to measure the signal (at f_o); $f_o > 0$

So, object is to keep Δf to a *minimum*,
without reducing the **SIGNAL**

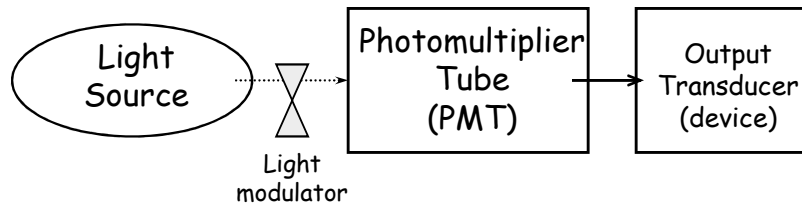
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Reducing 1/f Noise

- We need to *move* f_0 to >100 Hz . . . *HOW?*

→ **MODULATE** the source

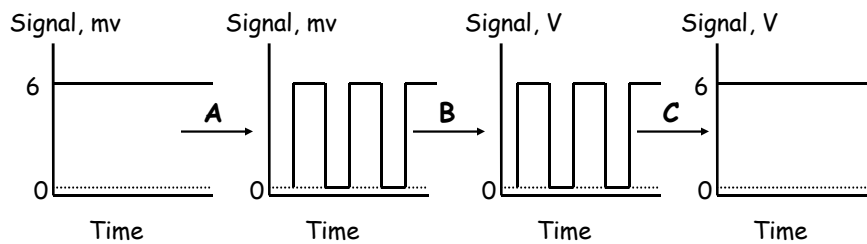
-analytical signal "encoded" at a freq.
where 1/f noise is negligible



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Tuned Amplification: *Chopper Amplifiers*

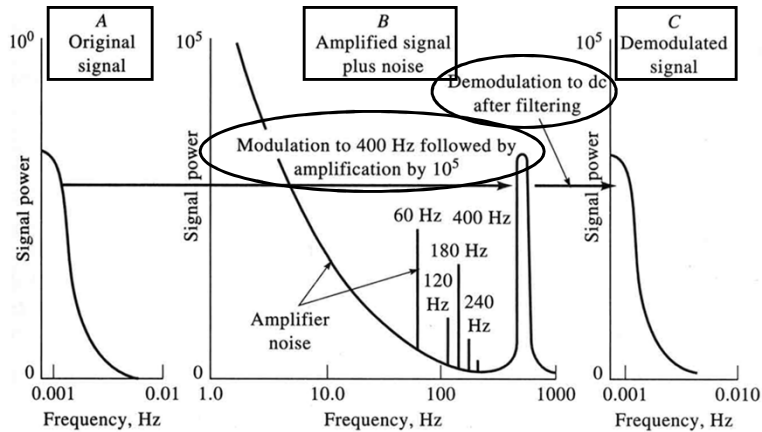
- If we *amplify* the signal at the modulation frequency, then we can also *increase the signal* while we *reduce the noise*:



A: modulate **B:** amplify **C:** demodulate

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Chopper Amplifiers: In the Frequency Domain



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Lock-In Amplification

- Tuned (chopper) amplification is limited by stability of f_0 reference
 - this limits the effective Δf to about 1 Hz
- *Lock-in* amplification tunes the amplifier to both f_0 as well as the phase of the signal
 - results in an effective reduction of Δf to about 0.01 Hz

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Signal Averaging

- Need a *repeatable* signal (time domain method)
- Sum digitally-stored replicate signals

- How does this improve S/N?

Signal: increases *linearly* with number (n) of replicate signals

Noise: increases as $(n)^{1/2}$

So, **S/N** increases as **$(n)^{1/2}$**

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Signal Averaging: Example

- Suppose we wish to *mass* a **10-mg** object on an analytical balance ($\sigma = 0.1 \text{ mg}$)

For a single (n = 1) measurement:

$$S = 10. \text{ mg}, N = 0.1 \text{ mg} \rightarrow \mathbf{S/N = 100}$$

For n = 4:

$$S = n \times 10. \text{ mg} = 4 \times 10. \text{ mg} = 40. \text{ mg}$$

$$N = \sigma_T = (n(\sigma)^2)^{1/2} = (4(0.1)^2)^{1/2} = 2(0.1) = 0.2 \text{ mg}$$

$$\mathbf{S/N = 40./0.2 = 200}$$

For n = 16: **S/N = 400**

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Signal Averaging: General

- In general, we can say:

$$(S/N)_n = (n)^{1/2} (S/N)_{n=1}$$

- Diminishing returns: *Suppose, it takes 1 second per measurement?*

<u>S/N</u>	<u>n</u>	<u>Time</u>
3	1	1 sec
6	4	4 sec
30	100	100 sec
300	10,000	2.8 <i>hours</i>
3000	1,000,000	11.6 <i>days</i>