

Chapter 6 - Categorical Data and Chi-Square

6.1 Popularity of psychology professors:

	Anderson	Klatsky	Kamm	Total
Observed	32	25	10	67
Expected	22.3	22.3	22.3	67

$$\begin{aligned}\chi^2 &= \sum \frac{(O - E)^2}{E} \\ &= \frac{(32 - 22.3)^2}{22.3} + \frac{(25 - 22.3)^2}{22.3} + \frac{(10 - 22.3)^2}{22.3} \\ &= 11.33^1\end{aligned}$$

Reject H_0 and conclude that students do not enroll at random.

6.3 Sorting one-sentence characteristics into piles:

	1	2	3	4	5	Total
Observed	8	10	20	8	4	50
Expected	5	10	20	10	5	50
Exp. %	10%	20%	40%	20%	10%	100%

$$\begin{aligned}\chi^2 &= \sum \frac{(O - E)^2}{E} \\ &= \frac{(8 - 5)^2}{5} + \frac{(10 - 10)^2}{10} + \frac{(20 - 20)^2}{20} + \frac{(8 - 10)^2}{10} + \frac{(4 - 5)^2}{5} \\ &= 2.4 \quad [\chi^2_{.05(4)} = 9.49]\end{aligned}$$

Do not reject H_0 that your friend's child's sorting behavior is in line with your theory.

¹ The answers to these questions may differ substantially, depending on the number of decimal places that are carried for the calculations. (e.g., for Exercise 6.18 answers can vary between 37.14 and 37.339.)

6.5 Racial choice in dolls (Clark & Clark, 1939):

	Black	White	Total
Observed	83	169	252
Expected	126	126	252

$$\begin{aligned}\chi^2 &= \sum \frac{(O-E)^2}{E} \\ &= \frac{(83-126)^2}{126} + \frac{(169-126)^2}{126} \\ &= 29.35 \quad [\chi^2_{.05(1)} = 3.84]\end{aligned}$$

Reject H_0 and conclude that the children did not chose dolls at random (at least with respect to color). It is interesting to note that this particular study played an important role in Brown v. Board of Education (1954). In that case the U.S. Supreme Court ruled that the principle of “separate but equal”, which had been the rule supporting segregation in the public schools, was no longer acceptable. Studies such as those of the Clarks had illustrated the negative effects of segregation on self-esteem and other variables.

6.7 Combining the two racial choice experiments:

Study	Black	White	Total
1939	83	169	252
	(106.42)	(145.58)	
1970	61	28	89
	(37.58)	(51.42)	
	144	197	341 = N

$$\begin{aligned}\chi^2 &= \sum \frac{(O-E)^2}{E} \\ &= \frac{(83-106.42)^2}{106.42} + \frac{(169-145.58)^2}{145.58} + \frac{(61-37.58)^2}{37.58} + \frac{(28-51.42)^2}{51.42} \\ &= 5.154 + 3.768 + 14.595 + 10.667 \\ &= 34.184 \quad [\chi^2_{.05(1)} = 3.84]\end{aligned}$$

Reject the H_0 and conclude that the distribution of choices between Black and White dolls was different in the two studies. Choice is *not* independent of Study. We are no longer asking whether one color of doll is preferred over the other color, but whether the *pattern* of preference is constant across studies. In analysis of variance terms we are dealing with an interaction.

- 6.9**
- a. Take a group of subjects at random and sort them by gender and life style (categorized three ways).
 - b. Deliberately take an equal number of males and females and ask them to specify a preference among 3 types of life style.
 - c. Deliberately take 10 males and 10 females and have them divide themselves into two teams of 10 players each.
- 6.11** Doubling the cell sizes:
- a. $\chi^2 = 10.306$
 - b. This demonstrates that the obtained value of χ^2 is exactly doubled, while the critical value remains the same. Thus the sample size plays a very important role, with larger samples being more likely to produce significant results—as is also true of other tests.
- 6.13** Gender and voting behavior

	Vote		Total
	Yes	No	
Women	35 (28.83)	9 (15.17)	44
Men	60 (66.17)	41 (34.83)	101
Total	95	50	145

$$\begin{aligned} \chi^2 &= \sum \frac{(O - E)^2}{E} \\ &= \frac{(35 - 28.83)^2}{28.83} + \frac{(9 - 15.17)^2}{15.17} + \frac{(60 - 66.17)^2}{66.17} + \frac{(41 - 34.83)^2}{34.83} \\ &= 5.50 \quad [\chi^2_{.05(1)} = 3.84] \end{aligned}$$

Reject H_0 and conclude that women voted differently from men. The odds that women would vote for civil unions were much greater than for men—the odds ratio is $(35/9)/(60/41) = 3.89/1.46 = 2.66$, meaning that women had 2.66 times the odds of voting for civil unions than men. That is a substantial difference, and likely reflects fundamental differences in attitude.

6.15 The relationship of assistance-seeking behavior to number of bystanders:

		Sought Assistance		Total
		Yes	No	
Number of Bystanders	0	11 (7.75)	2 (5.25)	13
	1	16 (15.5)	10 (10.5)	26
	4	4 (7.75)	9 (5.25)	13
			31	21

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

$$= \frac{(11 - 7.75)^2}{7.75} + \frac{(2 - 5.25)^2}{5.25} + \dots + \frac{(9 - 5.25)^2}{5.25}$$

$$= 7.908 \quad [\chi^2_{.05(2)} = 5.99]$$

Reject H_0 . The number of bystanders influences whether or not subjects seek help.

6.17 a. Weight preference in adolescent girls:

	Reducers	Maintainers	Gainers	Total
White	352 (336.7)	152 (151.9)	31 (46.4)	535
Black	47 (62.3)	28 (28.1)	24	99
		180	55 (8.6)	634 = N

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

$$= \frac{(352 - 336.7)^2}{336.7} + \frac{(152 - 151.9)^2}{151.9} + \dots + \frac{(24 - 8.6)^2}{8.6}$$

$$= 37.141 \quad [\chi^2_{.05(2)} = 5.99]$$

Adolescents girls' preferred weight varies with race.

- b. The number of girls desiring to lose weight was far in excess of the number of girls who were overweight.

6.19 Analyzing Exercise 6.12 (Regular or Remedial English and frequency of ADD diagnosis) using the likelihood-ratio approach:

	1st	2nd	4th	2 & 4	5th	2 & 5	4 & 5	2,4,&5	Total
Rem.	22	2	1	3	2	4	3	4	41
Reg.	187	17	11	9	16	7	8	6	261
	209	19	12	12	18	11	11	10	302

$$\chi^2 = 2 \left(\sum O_{ij} \ln \left[\frac{O_{ij}}{E_{ij}} \right] \right)$$

$$= 2 \times [22 \times \ln(22 / 28.374) + 2 \times \ln(2 / 2.579) + \dots + 6 \times \ln(6 / 8.642)]$$

$$= 2 \times [22(-.25443) + 2(-0.25444) + \dots + 6(-0.36492)]$$

$$= 12.753 \text{ on } 7 \text{ df}$$

Do not reject H_0 .

6.21 Monday Night Football opinions, before and after watching:

As the data are originally presented, chi-square would not be appropriate because the observations are not independent. The same subjects contribute twice to the data matrix.

6.23 b. Row percents take entries as a percentage of row totals, while column percents take entries as percentage of column totals.

c. These are the probabilities (to 4 decimal places) of a $\chi^2 \geq \chi^2_{\text{obt}}$

d. The correlation between the two variables is approximately .25.

6.25 For data in Exercise 6.24a:

a. $\phi_c = \sqrt{26.90 / 22,071} = 0.0349$

b. Odds Fatal | Placebo = 18/10,845 = .00166.

Odds Fatal | Aspirin = 5/10,933 = .000453.

Odds Ratio = .00166/.000453 = 3.598

The odds that you will die from a myocardial infarction are 3.6 times higher if you do not take aspirin than if you do.

6.27 For Table 6.4 the odds ratio for smoking as a function of gender is (150/350)/(100/400) = 1.7. The odds of men smoking are 1.7 times greater than for women.

For Table 6.5 the odds of being the primary shopper as a function of gender is (15/4)/(4/15) = 14.06. The odds of women being the primary shopper are 14.06 times the odds for men. This gender difference is much more extreme than it was for smoking.

6.29 Dabbs and Morris (1990) study of testosterone.

		Testosterone		
		High	Normal	Total
Delinquency	No	345 (395.723)	3614 (3563.277)	3959
	Yes	101 (50.277)	402 (452.723)	503
		446	4016	4462 = N

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

$$= \frac{(345 - 395.723)^2}{395.723} + \frac{(3614 - 3563.277)^2}{3563.277} + \frac{(101 - 50.277)^2}{50.277} + \frac{(402 - 452.723)^2}{452.723}$$

$$= 64.08 \quad [\chi^2_{.05(1)} = 3.84] \text{ Reject } H_0.$$

6.31 Childhood delinquency in the Dabbs and Morris (1990) study.

a.

		Testosterone		
		High	Normal	Total
Delinquency	No	366	3554	3920
		(391.824)	(3528.176)	
	Yes	80	462	542
		(54.176)	(487.824)	
		446	4016	4462 = N

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

$$= \frac{(366 - 391.824)^2}{391.824} + \frac{(3554 - 3528.176)^2}{3528.176} + \frac{(80 - 54.176)^2}{54.176} + \frac{(462 - 487.824)^2}{487.824}$$

$$= 15.57 \quad [\chi^2_{.05(1)} = 3.84] \text{ Reject } H_0.$$

- b. There is a significant relationship between high levels of testosterone in adult men and a history of delinquent behavior during childhood.
- c. This result shows that we can tie the two variables (delinquency and testosterone) together historically.

6.33 Good touch/Bad touch

a.

		Abused		Total
		Yes	No	
Received Program	Yes	43	457	500
		(56.85)	(443.15)	
	No	50	268	318
		(36.15)	(281.85)	
		93	725	818 = N

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

$$= \frac{(43 - 56.85)^2}{56.85} + \frac{(457 - 443.15)^2}{443.15} + \dots + \frac{(268 - 281.85)^2}{281.85}$$

$$= 9.79 \quad \chi^2_{.05(1)} = 3.84 \text{ Reject } H_0$$

b. Odds ratio

OR = $(43/457)/(50/268) = 0.094/0.186 = .505$. Those who receive the program have about half the odds of subsequently suffering abuse.

6.35 Gender of parents and children.

a.

		Lost Parent Gender		Total
		Male	Female	
Child	Male	18	34	52
	Female	27	61	88
		45	95	140 = <i>N</i>

$$\chi^2 = .232$$
$$(p = .630)$$

b. There is no relationship between the gender of the lost parent and the gender of the child.

c. We would be unable to separate effects due to parental gender from effects due to the child's gender. They would be completely confounded.

6.37 We could ask a series of similar questions, evenly split between “right” and “wrong” answers. We could then sort the replies into positive and negative categories and ask whether faculty were more likely than students to give negative responses.

6.39 I am trying to get you to think about the issues of measurement and about what we can, and cannot, tell from data. If scale points mean different things to different sexes, it is possible that the relationship could be distorted by the closed-end nature of the scales.