

Math 395 - Spring 2020  
Homework 5

This homework is due on Wednesday, February 19.

These problems can be turned in by hand:

Section 9.1: 4, 5

Section 9.2: 1, 5

Section 10.1: 1, 2, 8a

Section 10.2: 4, 5

This problem must be typed up:

1. Let  $F$  and  $K$  be finite fields with  $F \subseteq K$ . Let  $F[x]$  and  $K[x]$  denote the respective polynomial rings in the variable  $x$ , so  $F[x]$  is a subring of  $K[x]$ .
  - (a) Prove that if  $M$  is any maximal ideal in  $K[x]$ , then  $M \cap F[x]$  is a maximal ideal in  $F[x]$ .
  - (b) Give an explicit example of commutative rings  $A \subseteq B$  and a maximal ideal  $I$  of  $B$  such that  $I \cap A$  is not a maximal ideal of  $A$ .