

Math 295 - Spring 2020  
Homework 10

This homework is due on Wednesday, March 25. Most problems are adapted from Munkres's *Topology*.

1. Consider the *square metric*

$$\rho(\mathbf{x}, \mathbf{y}) = \max(|x_1 - y_1|, \dots, |x_n - y_n|),$$

for  $\mathbf{x} = (x_1, \dots, x_n), \mathbf{y} = (y_1, \dots, y_n) \in \mathbb{R}^n$ .

- (a) Show that  $\rho$  is a metric on  $\mathbb{R}^n$ .
  - (b) Show that  $\rho$  induces the standard topology on  $\mathbb{R}^n$ .
2. Show that every metric space is Hausdorff.
  3. Let  $X$  be a metric space with metric  $d$ , and  $A$  be a subspace of  $X$ .
    - (a) Show that  $d|_{A \times A}$  is a metric on  $A$ .
    - (b) Show that  $d|_{A \times A}$  induces the subspace topology on  $A$ .

No extra problem for graduate credit this week.