

Name:

**Problem 1:** Lemma 3 of Section 6 states that if  $p$  is an odd prime, then the least residues

$$2, 3, 4, \dots, p-4, p-3, p-2$$

can be partitioned into  $\frac{p-3}{2}$  pairs  $(a, a')$  such that for each pair,

$$aa' \equiv 1 \pmod{p},$$

with  $a \not\equiv a' \pmod{p}$ .

Let  $p = 11$ . Partition the set

$$\{2, 3, 4, 5, 6, 7, 8, 9\}$$

into four pairs  $(a, a')$  such that in each case  $aa' \equiv 1 \pmod{11}$ .