Name:

**Problem 1:** True or false: For positive integers m and n,

$$(m+n)! = m! + n!$$

If you answer "True," please provide a proof. If you answer "False," please provide a counter-example.

**Solution:** This is false, and almost every pair (m, n) will give a counter-example. Here is just one: m = 2, n = 3:

$$(2+3)! = 5! = 120 \neq 8 = 6+2 = 3! + 2!$$