Math 255 - Spring 2017
Homework 2
This homework is due on Monday, January 30.

1. (a) Use the Division Algorithm to show that the square of any integer is of the form $3 k$ or $3 k+1$.
(b) Use the Division Algorithm to show that the square of any integer is of the form $4 k$ or $4 k+1$.
2. Use induction to show that

$$
15 \mid\left(2^{4 n}-1\right) \text { for } n \geq 1
$$

3. Prove that if $a$ and $b$ are both odd integers, then $16 \mid\left(a^{4}+b^{4}-2\right)$.
