

Name:

Problem 1: Consider the matrix

$$A = \begin{pmatrix} 2 & -1 & 2 \\ -1 & 1 & 0 \\ 0 & -2 & -4 \\ 1 & 1 & 4 \\ -3 & 2 & -2 \end{pmatrix}.$$

- a) Write down the columns of the matrix A as separate vectors.
- b) The column space of A is a subspace of \mathbb{R}^n for some n . What is the value of n ?
- c) Is it possible for the column rank of A to be 4? Why or why not?
- d) Write down the rows of the matrix A as separate vectors.
- e) The row space of A is a subspace of \mathbb{R}^m for some m . What is the value of m ?

There is another question on the back.

f) Is it possible for the row rank of A to be 4? Why or why not?