Overview of Complex Networks

Last updated: 2023/08/22, 11:48:25 EDT

Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 6701, 6713, & a pretend number, 2023–2024| @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center Santa Fe Institute | University of Vermont



Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License.

The PoCSverse Overview of Complex Networks 1 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



These slides are brought to you by:

Sealie & Lambie Productions

The PoCSverse Overview of Complex Networks 2 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



These slides are also brought to you by:

Special Guest Executive Producer



On Instagram at pratchett_the_cat

The PoCSverse Overview of Complex Networks 3 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Outline

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

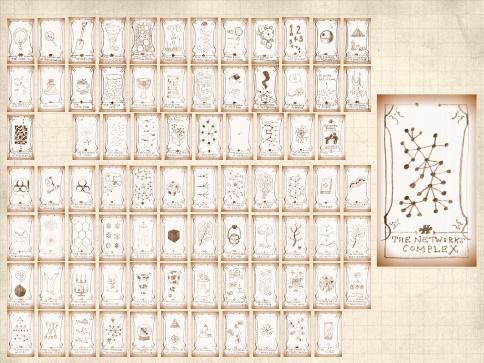
References

The PoCSverse Overview of Complex Networks 4 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks





Outline

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Physical networks Interaction networks Relational networks The PoCSverse Overview of Complex Networks 6 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



net•work |'net_iwərk|

noun

1 an arrangement of intersecting horizontal and vertical lines.

• a complex system of roads, railroads, or other transportation routes : *a network of railroads*.

2 a group or system of interconnected people or things : a trade network.

- a group of people who exchange information, contacts, and experience for professional or social purposes : a support network.
- a group of broadcasting stations that connect for the simultaneous broadcast of a program : the introduction of a second TV network | [as adj.] network television.
- a number of interconnected computers, machines, or operations : *specialized computers that manage multiple outside connections to a network* | *a local cellular phone network*.
- a system of connected electrical conductors.

verb [trans.]

connect as or operate with a network : the stock exchanges have proven to be resourceful in networking these deals.

• link (machines, esp. computers) to operate interactively : [as adj.] (**networked**) networked workstations.

• [intrans.] [often as n.] (**networking**) interact with other people to exchange information and develop contacts, esp. to further one's career : *the skills of networking, bargaining, and negotiation.*

The PoCSverse Overview of Complex Networks 7 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Thesaurus deliciousness:

network

noun

 a network of arteries WEB, lattice, net, matrix, mesh, crisscross, grid, reticulum, reticulation; Anatomy plexus.
 a network of lanes MAZE, labyrinth, warren, tangle.
 a network of friends SYSTEM, complex, nexus, web, webwork. The PoCSverse Overview of Complex Networks 8 of 43

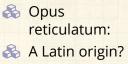
Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



From Keith Briggs's excellent etymological investigation:





[http://serialconsign.com/2007/11/we-put-net-

network]

The PoCSverse Overview of Complex Networks 9 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

The PoCSverse Overview of Complex Networks 10 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

🚳 1658–: reticulate structures in animals

The PoCSverse Overview of Complex Networks 10 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

A 1658-: reticulate structures in animals 1839-: rivers and canals The PoCSverse Overview of Complex Networks 10 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

1658-: reticulate structures in animals
1839-: rivers and canals
1869-: railways

The PoCSverse Overview of Complex Networks 10 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

- 🚳 1658–: reticulate structures in animals
- \lambda 1839–: rivers and canals
- 🚳 1869–: railways
- 🚳 1883–: distribution network of electrical cables

The PoCSverse Overview of Complex Networks 10 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

- 🚳 1658–: reticulate structures in animals
- 🚳 1839–: rivers and canals
- 🚳 1869–: railways
- 🗞 1883–: distribution network of electrical cables
- 🗞 1914–: wireless broadcasting networks

The PoCSverse Overview of Complex Networks 10 of 43

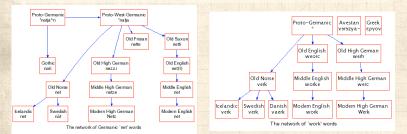
Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- 888).
- Work' appear to have long meant purposeful action.



The PoCSverse Overview of Complex Networks 11 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

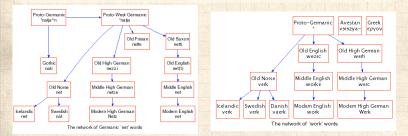
Examples of Complex Networks Physical networks Interaction networks Relational networks



Ancestry: Net and Work are venerable old words: 'Net' first used to mean spider web (King Ælfréd,

888).

Work' appear to have long meant purposeful action.



'Network' = something built based on the idea of natural, flexible lattice or web. The PoCSverse Overview of Complex Networks 11 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

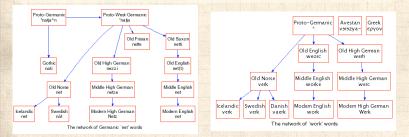
Examples of Complex Networks Physical networks Interaction networks Relational networks



Ancestry: Net and Work are venerable old words: 'Net' first used to mean spider web (King Ælfréd,

888).

Work' appear to have long meant purposeful action.



'Network' = something built based on the idea of natural, flexible lattice or web.

🗞 c.f., ironwork, stonework, fretwork.

The PoCSverse Overview of Complex Networks 11 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Many complex systems can be viewed as complex networks of physical or abstract interactions. The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.



Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...



Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- largely due to your typical theoretical physicist:

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- …largely due to your typical theoretical physicist:



👌 Piranha physicus

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- …largely due to your typical theoretical physicist:



Piranha physicus

Hunt in packs.

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- …largely due to your typical theoretical physicist:



- 👌 Piranha physicus
- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- largely due to your typical theoretical physicist:



- 🖻 Piranha physicus
- 🝞 Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)



See also: https://xkcd.com/793/

The PoCSverse Overview of Complex Networks 12 of 43

Complex Networks Basics

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Outline

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

> Physical networks Interaction networks Relational networks

The PoCSverse Overview of Complex Networks 13 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Popularity (according to Google Scholar)



"Collective dynamics of 'small-world' networks" Watts and Strogatz, Nature, **393**, 440–442, 1998.^[16]

Times cited:

(as of October 24, 2018)

The PoCSverse Overview of Complex Networks 14 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

References



"Emergence of scaling in random networks" Barabási and Albert, Science, **286**, 509–511, 1999.^[2]

Times cited:

(as of October 24, 2018)



Popularity (according to Google Scholar)



"Collective dynamics of 'small-world' networks" Watts and Strogatz, Nature, **393**, 440–442, 1998.^[16]

Times cited: $\Box \sim 37,460$ (as of October 24, 2018)

The PoCSverse Overview of Complex Networks 14 of 43

Complex Networks Basics

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

References



"Emergence of scaling in random networks" Barabási and Albert, Science, **286**, 509–511, 1999.^[2]

Times cited:

(as of October 24, 2018)



Popularity (according to Google Scholar)



"Collective dynamics of 'small-world' networks" Watts and Strogatz, Nature, **393**, 440–442, 1998.^[16]

Times cited: $\Box \sim 37,460$ (as of October 24, 2018)



"Emergence of scaling in random networks" Barabási and Albert, Science, **286**, 509–511, 1999.^[2]

Times cited: 27 ~ 32,093 (as of October 24, 2018)

The PoCSverse Overview of Complex Networks 14 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Review articles:



"Complex Networks: Structure and Dynamics" Boccaletti et al., Physics Reports, **424**, 175–308, 2006. ^[3]

Times cited: 🗹 ~ 8,533 (as of October 24, 2018)



"The structure and function of complex networks" M. E. J. Newman, SIAM Rev., **45**, 167–256, 2003.^[12]

Times cited: C ~ 17,782 (as of October 24, 2018)



"Statistical mechanics of complex networks" Albert and Barabási, Rev. Mod. Phys., **74**, 47–97, 2002. ^[1]

Times cited: C ~ 20,531 (as of October 24, 2018)

The PoCSverse Overview of Complex Networks 15 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Popularity according to textbooks:

The PoCSverse Overview of Complex Networks 16 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Popularity according to textbooks:



"Networks" **3** C by Mark Newman (2018).^[11]



DAVID EASLEY and JON KLEINBERG



"Networks, crowds, and markets: Reasoning about a highly connected world" **3**, by Easley and Kleinberg (2010). ^[7]

http://cs.cornell.edu/home/kleinber/networks-book/

THE NETWORK

The PoCSverse Overview of Complex Networks 16 of 43

Complex Networks Basics

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

Popularity according to books:



GLADWELL

(it is different into " - Political

The Tipping Point: How Little Things can make a Big Difference—Malcolm Gladwell^[8]



Nexus: Small Worlds and the Groundbreaking Science of Networks—Mark Buchanan

THE NETWORK

The PoCSverse Overview of Complex Networks 17 of 43

Complex Networks Basics Etymology

Popularity Graph theory?

Examples of Complex Networks Physical networks Interaction networks Relational networks

Popularity according to books:

Haw Everything In Connected to Exceptions Else and What Is Means for Datasets, Science, and Everyday Life

Linked

Albert-Lészlő Berebési

Linked: How Everything Is Connected to Everything Else and What It Means—Albert-Laszlo Barabási Overview of Complex Networks 18 of 43

The PoCSverse

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

References



Six Degrees: The Science of a Connected Age—Duncan Watts^[15]



Numerous others ...

- Complex Social Networks—F. Vega-Redondo^[14]
- Fractal River Basins: Chance and Self-Organization—I. Rodríguez-Iturbe and A. Rinaldo^[13]
- 🗞 Random Graph Dynamics—R. Durette
- 🚳 Scale-Free Networks—Guido Caldarelli
- Evolution and Structure of the Internet: A Statistical Physics Approach—Romu Pastor-Satorras and Alessandro Vespignani
- 🚳 Complex Graphs and Networks—Fan Chung
- Social Network Analysis—Stanley Wasserman and Kathleen Faust
- Handbook of Graphs and Networks—Eds: Stefan Bornholdt and H. G. Schuster^[5]
- Evolution of Networks—S. N. Dorogovtsev and J. F. F. Mendes^[6]

The PoCSverse Overview of Complex Networks 19 of 43

Complex Networks Basics Etymology

Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Outline

Complex Networks Basics

Popularity Graph theory?

Physical networks Interaction networks Relational networks The PoCSverse Overview of Complex Networks 20 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ...

The PoCSverse Overview of Complex Networks 21 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Relational networks



But surely networks aren't new ...
Graph theory is well established ...

The PoCSverse Overview of Complex Networks 21 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ...
Graph theory is well established ...
Study of social networks started in the 1930's ...



Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ...
Graph theory is well established ...
Study of social networks started in the 1930's ...
So why all this 'new' research on networks?



Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ...
Graph theory is well established ...
Study of social networks started in the 1930's ...
So why all this 'new' research on networks?
Answer: Oodles of Easily Accessible Data.



Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ...
Graph theory is well established ...
Study of social networks started in the 1930's ...
So why all this 'new' research on networks?
Answer: Oodles of Easily Accessible Data.
We can now inform (alas) our theories with a much more measurable reality.*

The PoCSverse Overview of Complex Networks 21 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



- But surely networks aren't new ...
 Graph theory is well established ...
 Study of social networks started in the 1930's ...
 So why all this 'new' research on networks?
 Answer: Oodles of Easily Accessible Data.
 We can now inform (alas) our theories with a much more measurable reality.*
- A worthy goal: establish mechanistic explanations.

The PoCSverse Overview of Complex Networks 21 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



But surely networks aren't new ... Graph theory is well established ... 🚓 Study of social networks started in the 1930's ... So why all this 'new' research on networks? Answer: Oodles of Easily Accessible Data. 🚳 We can now inform (alas) our theories with a much more measurable reality.* A worthy goal: establish mechanistic explanations. *If this is upsetting, maybe string theory is for you ...

The PoCSverse Overview of Complex Networks 21 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



🗞 Web-scale data sets can be overly exciting.

The PoCSverse Overview of Complex Networks 22 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Web-scale data sets can be overly exciting.

Witness:

The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired) The PoCSverse Overview of Complex Networks 22 of 43

Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Web-scale data sets can be overly exciting.

Witness:

- The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired)
- "The Unreasonable Effectiveness of Data," Halevy et al. ^[9].
- c.f. Wigner's "The Unreasonable Effectiveness of Mathematics in the Natural Sciences" [17]

The PoCSverse Overview of Complex Networks 22 of 43

Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Web-scale data sets can be overly exciting.

Witness:

- The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired)
- "The Unreasonable Effectiveness of Data," Halevy et al. ^[9].
- c.f. Wigner's "The Unreasonable Effectiveness of Mathematics in the Natural Sciences" [17]

But:

line for scientists, description is only part of the battle.

The PoCSverse Overview of Complex Networks 22 of 43

Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Web-scale data sets can be overly exciting.

Witness:

- The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired)
- "The Unreasonable Effectiveness of Data," Halevy et al. ^[9].
- c.f. Wigner's "The Unreasonable Effectiveness of Mathematics in the Natural Sciences" [17]

But:

For scientists, description is only part of the battle.We still need to understand.

The PoCSverse Overview of Complex Networks 22 of 43

Complex Networks Basics Etymology

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Outline

Complex Networks Basics

Graph theory? Basic definitions

Physical networks Interaction networks Relational networks The PoCSverse Overview of Complex Networks 23 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other

The PoCSverse Overview of Complex Networks 24 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other

e.g., people, forks in rivers, proteins, webpages, organisms, ...

The PoCSverse Overview of Complex Networks 24 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other

e.g., people, forks in rivers, proteins, webpages, organisms, ...

Links = Connections between nodes

The PoCSverse Overview of Complex Networks 24 of 43

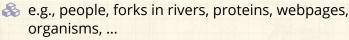
Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other



Links = Connections between nodes Links may be directed or undirected. The PoCSverse Overview of Complex Networks 24 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other

e.g., people, forks in rivers, proteins, webpages, organisms, ...

Links = Connections between nodes

Links may be directed or undirected.
 Links may be binary or weighted.

The PoCSverse Overview of Complex Networks 24 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Nodes = A collection of entities which have properties that are somehow related to each other

e.g., people, forks in rivers, proteins, webpages, organisms, ...

Links = Connections between nodes

Links may be directed or undirected.
 Links may be binary or weighted.

Other spiffing words: vertices and edges.

The PoCSverse Overview of Complex Networks 24 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity

Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node Notation: Node *i*'s degree = k_i .

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

Solution: Node *i*'s degree = k_i . $k_i = 0,1,2,...$ The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

- \aleph Notation: Node *i*'s degree = k_i .
- $k_i = 0, 1, 2,$
- \aleph Notation: the average degree of a network = $\langle k \rangle$

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

- \aleph Notation: Node *i*'s degree = k_i .
- $k_i = 0, 1, 2, \dots$
- Solution: the average degree of a network = $\langle k \rangle$ (and sometimes z)

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

- \aleph Notation: Node *i*'s degree = k_i .
- $\& k_i = 0, 1, 2,$
- Notation: the average degree of a network = $\langle k \rangle$ (and sometimes *z*)
- Connection between number of edges m and average degree:

$$\langle k \rangle = \frac{2m}{N}.$$

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Node degree = Number of links per node

- \aleph Notation: Node *i*'s degree = k_i .
- $\& k_i = 0, 1, 2, \dots$
- Notation: the average degree of a network = $\langle k \rangle$ (and sometimes *z*)
- Connection between number of edges m and average degree:

$$\langle k \rangle = \frac{2m}{N}.$$

 \mathfrak{S} Defn: \mathcal{N}_i = the set of *i*'s k_i neighbors

The PoCSverse Overview of Complex Networks 25 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Adjacency matrix:

We represent a directed network by a matrix A with link weight a_{ij} for nodes i and j in entry (i, j).

The PoCSverse Overview of Complex Networks 26 of 43

Complex Networks Basics Etymology Popularity Graph theory?

Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Adjacency matrix:

We represent a directed network by a matrix A with link weight a_{ij} for nodes i and j in entry (i, j).
 e.g.,

$$A = \begin{bmatrix} 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix}$$

The PoCSverse Overview of Complex Networks 26 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



Adjacency matrix:

We represent a directed network by a matrix A with link weight a_{ij} for nodes i and j in entry (i, j).
 e.g.,

	Γ0	1	1	1	0 -	1
	$\begin{bmatrix} 0\\0\\1\\0\\0 \end{bmatrix}$	0	1	0	1	
A =	1	0	0	0	0	
	0	1	0	0	1	
		1	0	1	0 _	

The PoCSverse Overview of Complex Networks 26 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

References

(n.b., for numerical work, we always use sparse matrices.)



So what passes for a complex network?

The PoCSverse Overview of Complex Networks 27 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Interaction networks Relational networks



The PoCSverse Overview of Complex Networks 27 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Interaction networks Relational networks



So what passes for a complex network?

Complex networks are large (in node number)
 Complex networks are sparse (low edge to node ratio)

The PoCSverse Overview of Complex Networks 27 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Relational networks



So what passes for a complex network?

- lin node number)
- Complex networks are sparse (low edge to node ratio)
- Complex networks are usually dynamic and evolving

The PoCSverse Overview of Complex Networks 27 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks

Relational networks References



So what passes for a complex network?

- lin node number) 🚳
- Complex networks are sparse (low edge to node ratio)
- Complex networks are usually dynamic and evolving
- Complex networks can be social, economic, natural, informational, abstract, ...

The PoCSverse Overview of Complex Networks 27 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks



Outline

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Interaction networks Relational networks The PoCSverse Overview of Complex Networks 28 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks

🚳 River networks



The PoCSverse Overview of Complex Networks 29 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks

River networksNeural networks



The PoCSverse Overview of Complex Networks 29 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks

River networks
Neural networks
Trees and leaves





The PoCSverse Overview of Complex Networks 29 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks

River networks
Neural networks
Trees and leaves
Blood networks





The PoCSverse Overview of Complex Networks 29 of 43

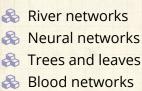
Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Physical networks Interaction networks Relational networks

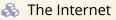


Physical networks











The PoCSverse Overview of Complex Networks 29 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

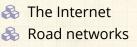
Physical networks Interaction networks Relational networks



Physical networks



🙈 River networks 🙈 Neural networks Trees and leaves Blood networks









The PoCSverse Overview of Complex Networks 29 of 43

Networks Basics Etymology Popularity Graph theory?

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks



🙈 River networks 🙈 Neural networks Trees and leaves Blood networks

🚳 The Internet 🙈 Road networks \lambda Power grids







The PoCSverse Overview of Complex Networks 29 of 43

Networks Basics Etymology Popularity Graph theory?

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Physical networks



🙈 River networks 🙈 Neural networks A Trees and leaves Blood networks

🚳 The Internet Road networks \lambda Power grids







Distribution (branching) versus redistribution (cyclical)

The PoCSverse Overview of Complex Networks 29 of 43

Networks Basics Etymology Graph theory?

Examples of Complex Networks

Physical networks Interaction networks Relational networks



Outline

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks The PoCSverse Overview of Complex Networks 30 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

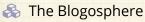
Examples of Complex Networks

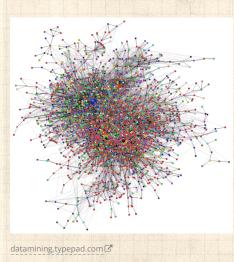
Physical networks

Interaction networks Relational networks



Interaction networks





The PoCSverse Overview of Complex Networks 31 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Interaction networks Relational networks



Interaction networks

🚳 The Blogosphere Biochemical networks



The PoCSverse Overview of Complex Networks 31 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Interaction networks Relational networks



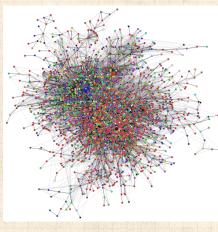
Interaction networks



🚳 The Blogosphere 🙈 Biochemical

networks

🚳 Gene-protein networks



datamining.typepad.com

The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks

Interaction networks Relational networks



Interaction networks



- 🚳 The Blogosphere
- 🙈 Biochemical networks
- 🚳 Gene-protein networks
- 🙈 Food webs: who eats whom



datamining.typepad.com

The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks Physical networks

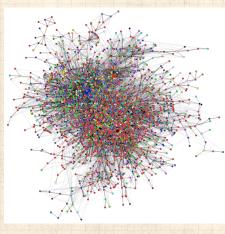
Interaction networks Relational networks



Interaction networks



- 🚳 The Blogosphere
- 🙈 Biochemical networks
- 🚳 Gene-protein networks
- 🙈 Food webs: who eats whom
- 🙈 The World Wide Web (?)



datamining.typepad.com

The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks Physical networks

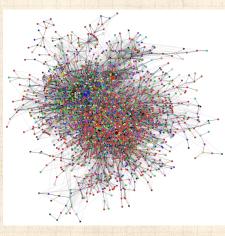
Interaction networks Relational networks



Interaction networks



- 🗞 The Blogosphere
- 🙈 Biochemical networks
- 🚳 Gene-protein networks
- 🙈 Food webs: who eats whom
- 🙈 The World Wide Web (?)
- 🙈 Airline networks



datamining.typepad.com

The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks Physical networks

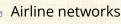
Interaction networks Relational networks



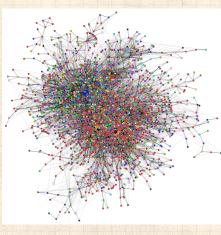
Interaction networks



- 🚳 The Blogosphere
 - Biochemical networks
- 🚳 Gene-protein networks
- 🙈 Food webs: who eats whom
- 🙈 The World Wide Web (?)



Call networks (AT&T)



datamining.typepad.com

The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

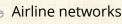
Interaction networks Relational networks



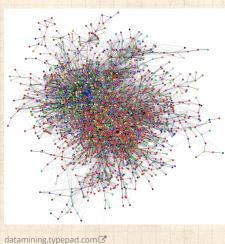
Interaction networks



- 🚳 The Blogosphere
 - Biochemical networks
- 🚳 Gene-protein networks
- 🙈 Food webs: who eats whom
- 🙈 The World Wide Web (?)



Call networks (AT&T)🙈 The Media



The PoCSverse Overview of Complex Networks 31 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Networks

Interaction networks Relational networks



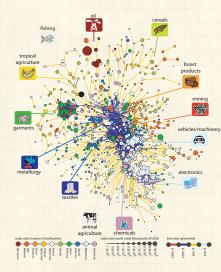
topics:

3

Hidalgo et al.'s "The Product Space Conditions the Development of Nations" ^[10]

How do products depend on each other, and how does this network evolve?

How do countries depend on each other for water, energy, people (immigration), investments?



The PoCSverse Overview of Complex Networks 32 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

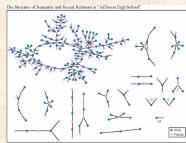
Examples of Complex Networks Physical networks Interaction networks



Interaction networks: social networks



🚳 Snogging



Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Physical networks

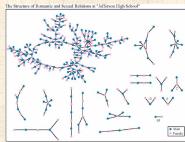
Interaction networks Relational networks



Interaction networks: social networks



🚳 Snogging 🚳 Friendships



preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Physical networks

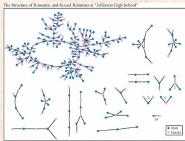
Interaction networks Relational networks



Interaction networks: social networks



- 🚳 Snogging 🗞 Friendships
- 🚳 Acquaintances



preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Physical networks

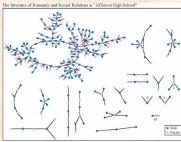
Interaction networks Relational networks



Interaction networks: social networks



- \delta Snogging
- \lambda Friendships
- \lambda Acquaintances
- Boards and directors



preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Physical networks

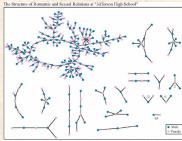
Interaction networks Relational networks



Interaction networks: social networks



- \delta Snogging
- \lambda Friendships
- \lambda Acquaintances
- Boards and directors
- \lambda Organizations



preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Interaction networks Relational networks

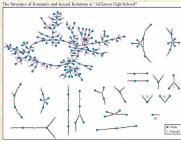


Interaction networks: social networks



- \delta Snogging
- \lambda Friendships
- \lambda Acquaintances
- Boards and directors

\lambda Organizations 🚳 facebook 🗹 twitter 📿 ,



Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

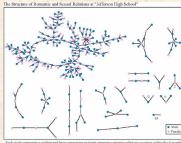
Interaction networks Relational networks



Interaction networks: social networks



- 🚳 Snogging
- \lambda Friendships
 - Acquaintances
 - Boards and directors
- Organizations 😤 facebook 🖸 twitter 🖸



Each circle represents a student and lines connecting students represent remantic relations occuring within the 6 month preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Etymology Graph theory? Basic definitions

Examples of Complex Networks

Interaction networks

References

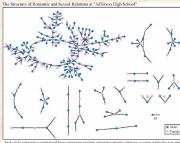
🚳 'Remotely sensed' by: email activity, instant messaging, phone logs



Interaction networks: social networks



- 🚳 Snogging
- \lambda Friendships
 - Acquaintances
 - Boards and directors
- Organizations 😤 facebook 🖸 twitter 🖸



Each circle represents a student and lines connecting students represent remantic relations occuring within the 6 month preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

The PoCSverse Overview of Complex Networks 33 of 43

Networks Basics Graph theory? Basic definitions

Examples of Complex Networks

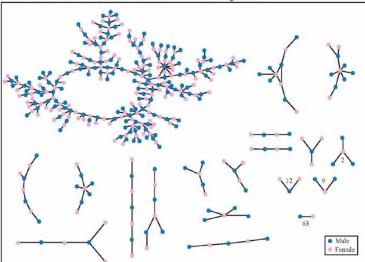
Interaction networks

References

🚳 'Remotely sensed' by: email activity, instant messaging, phone logs (*cough*).



The Structure of Romantic and Sexual Relations at "Jefferson High School"



Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

The PoCSverse Overview of Complex Networks 34 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks

Interaction networks Relational networks



Outline

Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks The PoCSverse Overview of Complex Networks 35 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Relational networks

🚳 Consumer purchases

The PoCSverse Overview of Complex Networks 36 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Relational networks

Consumer purchases (Walmart, Target, Amazon, ...) The PoCSverse Overview of Complex Networks 36 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Relational networks

- Consumer purchases (Walmart, Target, Amazon, ...)
- Thesauri: Networks of words generated by meanings

The PoCSverse Overview of Complex Networks 36 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Relational networks

- Consumer purchases (Walmart, Target, Amazon, ...)
- Thesauri: Networks of words generated by meanings
- 🗞 Knowledge/Databases/Ideas



Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Relational networks

- Consumer purchases (Walmart, Target, Amazon, ...)
- Thesauri: Networks of words generated by meanings
- 🗞 Knowledge/Databases/Ideas
- 🚳 Metadata—Tagging: bit.ly 🗹 flickr 🗹

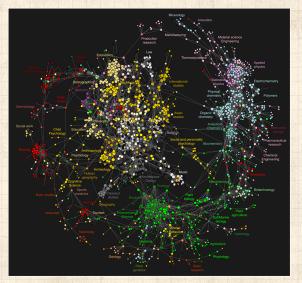
common tags cloud | list

community daily dictionary education **encyclopedia** english free imported info information internet knowledge learning news **reference** research resource resources search tools useful web web2.0 **Wiki wikipedia** The PoCSverse Overview of Complex Networks 36 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions



Clickworthy Science:



The PoCSverse Overview of Complex Networks 37 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks References



"Clickstream Data Yields High-Resolution Maps of Science", Bollen et al. ^[4], 2009.

Neural reboot (NR):

Dog has fun.

The PoCSverse Overview of Complex Networks 38 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks References

https://www.youtube.com/watch?v=7xEX-48RHCY?rel=0



References I

 R. Albert and A.-L. Barabási. Statistical mechanics of complex networks. Rev. Mod. Phys., 74:47–97, 2002. pdf

[2] A.-L. Barabási and R. Albert. Emergence of scaling in random networks. Science, 286:509–511, 1999. pdf 7

 S. Boccaletti, V. Latora, Y. Moreno, M. Chavez, and D.-U. Hwang.
 Complex networks: Structure and dynamics. Physics Reports, 424:175–308, 2006. pdf

The PoCSverse Overview of Complex Networks 39 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



References II

J. Bollen, H. Van de Sompel, A. Hagberg,
 L. Bettencourt, R. Chute, M. A. Rodriguez, and
 B. Lyudmila.
 Clickstream data yields high-resolution maps of science.
 PLOS ONE, 4:e4803, 2009. pdf C

[5] S. Bornholdt and H. G. Schuster, editors. Handbook of Graphs and Networks. Wiley-VCH, Berlin, 2003.

[6] S. N. Dorogovtsev and J. F. F. Mendes. <u>Evolution of Networks</u>. Oxford University Press, Oxford, UK, 2003. The PoCSverse Overview of Complex Networks 40 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



References III

- [7] D. Easley and J. Kleinberg.
 <u>Networks</u>, crowds, and markets: Reasoning about a highly connected world.
 <u>Cambridge University Press</u>, 2010.
- [8] M. Gladwell. <u>The Tipping Point.</u> Little, Brown and Company, New York, 2000.
- [9] A. Halevy, P. Norvig, and F. Pereira. The unreasonable effectiveness of data. IEEE Intelligent Systems, 24:8–12, 2009. pdf C.
- [10] C. A. Hidalgo, B. Klinger, A.-L. Barabási, and R. Hausman. The product space conditions the development of nations. <u>Science</u>, 317:482–487, 2007. pdf 7

The PoCSverse Overview of Complex Networks 41 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



References IV

[11] M. Newman. <u>Networks</u>. Oxford university press, 2nd edition, 2018.

[12] M. E. J. Newman. The structure and function of complex networks. SIAM Rev., 45(2):167–256, 2003. pdf

 [13] I. Rodríguez-Iturbe and A. Rinaldo.
 Fractal River Basins: Chance and Self-Organization.
 Cambridge University Press, Cambrigde, UK, 1997.

[14] F. Vega-Redondo. <u>Complex Social Networks</u>. Cambridge University Press, 2007. The PoCSverse Overview of Complex Networks 42 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks



References V

[15] D. J. Watts. <u>Six Degrees</u>. Norton, New York, 2003.

[16] D. J. Watts and S. J. Strogatz. Collective dynamics of 'small-world' networks. Nature, 393:440–442, 1998. pdf 7

 [17] E. Wigner. The unreasonable effectivenss of mathematics in the natural sciences. <u>Communications on Pure and Applied</u> <u>Mathematics</u>, 13:1–14, 1960. pdf ^C The PoCSverse Overview of Complex Networks 43 of 43

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

