

Prediction and predictability of global epidemics: the role of the airline transportation network

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Abstract

The systematic study of large-scale networks has unveiled the ubiquitous presence of connectivity patterns characterized by large scale heterogeneities and unbounded statistical fluctuations. These features affect dramatically the behavior of the diffusion processes occurring on networks, determining the ensuing statistical properties of their evolution pattern and dynamics. In this paper, we investigate the role of the large scale properties of the airline transportation network in determining the global evolution of emerging disease. We present a stochastic computational framework for the forecast of global epidemics that considers the complete world-wide air travel infrastructure complemented with census population data. We address two basic issues in global epidemic modeling: i) We study the role of the large scale properties of the airline transportation network in determining the global diffusion pattern of emerging diseases; ii) We evaluate the reliability of forecasts and outbreak scenarios with respect to the intrinsic stochasticity of disease transmission and traffic flows. In order to address these issues we define a set of novel quantitative measures able to characterize the level of heterogeneity and predictability of the epidemic pattern. These

measures may be used for the analysis of containment policies and epidemic risk assessment.

The mathematical modeling of epidemics has often dealt with the predictions and predictability of outbreaks in real populations with complicated social and spatial structures and with heterogeneous patterns in the contact network [1, 2, 3, 4, 5, 6, 7, 8]. All these factors have led to sophisticated modeling approaches including disease realism, meta-population grouping, stochasticity and more recently to agent based numerical simulations that recreate entire populations and their dynamics at the scale of the single individual [9, 10]. In many instances however the introduction of the inherent complex features and emerging properties [11, 12, 13] of the network in which epidemics occur implies the breakdown of standard homogeneous approaches [5, 6] and calls for a systematic investigation of the impact of the detailed system's characteristics in the evolution of the epidemic outbreak. These considerations are particularly relevant in the study of the geographical spread of epidemics where the various long-range heterogeneous connections typical of modern transportation networks naturally give rise to a very complicated evolution of epidemics characterized by heterogeneous and seemingly erratic outbreaks [14, 15], as recently documented in the SARS case [16]. In this context, air-transportation represents a major channel of epidemic propagation, as pointed out in the modeling approach to global epidemic diffusion of Rvachev and Longini [17] capitalizing on previous studies on the Russian airline network [18]. Similar modeling approaches, even if limited by a very partial knowledge of the world-wide transportation network, have been used to study specific outbreaks such as pandemic influenza [19, 20, 21], HIV [22], and very recently SARS [23]. The availability of the complete world-wide airport network (*WAN*) dataset and the recent extensive studies of its topology [24, 25] are finally allowing a full scale computational study of global epidemics. In the following we will consider for the first time a global stochastic epidemic model including the full International Air Transport Association (*IATA*) [26] database, aiming at a detailed study of the interplay among the network structure and the

stochastic features of the infection dynamics in defining the global spreading of epidemics. In particular, while previous studies have generally been focused in the *a-posteriori* analysis of real case studies of global epidemics, the large scale modeling presented here allows us to address more basic theoretical issues such as the statistical properties of the epidemic pattern and the effect on it of the complex architecture of the underlying transportation network. Finally such a detailed level of description allows for the first time the quantitative assessment of the reliability of the obtained forecast with respect to the stochastic nature of the disease transmission and travel flows, the outbreak initial conditions and the network structure.

The air transportation network

In the following we use the International Air Transport Association (IATA) [26] database containing the world list of airport pairs connected by direct flights and the number of available seats on any given connection for the year 2002. The resulting world-wide air-transportation network (WAN) is therefore a weighted graph comprising $V = 3880$ vertices denoting airports and $E = 18810$ weighted edges whose weight $w_{j\ell}$ accounts for the passenger flow between the airports j and ℓ . This dataset has been complemented by the population N_j of the large metropolitan area served by the airport as obtained by different sources. The final network dataset contains the 3100 largest airports, 17182 edges (accounting for 99% of the worldwide traffic) and the respective urban population data. The obtained network is highly heterogeneous both in the connectivity pattern and the traffic capacities (see Fig. 1). The probability distributions that an airport j has k_j connections (degree) to other airports and handles a number $T_j = \sum_{\ell} w_{j\ell}$ of passengers (traffic) exhibit heavy-tails and very large statistical fluctuations [25, 24]. Analogously, the probability that a connection has a traffic w is skewed and heavy-tailed. Finally, we associate to each airport a city whose population N is heavy-tailed distributed in agreement with the general result of Zipf's law for the city size [27]. More strikingly, these quantities appear to have non-linear associations among them. This is clearly shown by the behavior relating the traffic handled by each airport T with the corresponding number of

connections k that follows the non-linear form $T \sim k^\beta$ with $\beta \simeq 1.5$ [24]. Analogously, the city population and the traffic handled by the corresponding airport follows the non-linear relation $N \sim T^\alpha$ with $\alpha \simeq 0.5$ in contrast with the linear behavior assumed in previous analysis [23]. The presence of broad statistical distributions and non-linear relations among the various quantities indicate a possible major impact in the ensuing disease spreading pattern.

Modeling global epidemics

As a basic element of our modeling approach we assume the basic standard compartmentalization in which each individual can only exist in one of the discrete states such as susceptible (S), latent (L), infected (I), permanently recovered (R), etc. In each city j the population is N_j and $X_j^{[m]}(t)$ is the number of individuals in the class $[m]$ at time t . By definition it follows that $N_j = \sum_m X_j^{[m]}(t)$. In each city j the individuals are allowed to travel from one city to another by means of the airline transportation network and to change compartment because of the infection dynamics in each city, similarly to the models in refs. [17, 20, 22] and the stochastic generalization of ref. [23].

Transport operator. The dynamics of individuals due to travels between cities is described by the transport operator $\Omega_j(\{X^{[m]}\})$ representing the net balance of individuals in a given class $X^{[m]}$ that entered and left each city j . This operator is a function of the traffic flows $w_{j\ell}$ per unit time, the city populations N_j , and might also include transit passengers on connecting flights. The number of passengers of each category traveling from a city j to a city ℓ is an integer random variable, in that each of the $X_j^{[m]}$ potential travellers has a probability $p_{j\ell} = w_{j\ell}\Delta t/N_j$ to go from j to ℓ in the time interval Δt . In each city j the numbers of passengers $\xi_{j\ell}$ traveling on each connection $j \rightarrow \ell$ at time t define a set of stochastic variables which follow the multinomial

distribution

$$P(\{\xi_{j\ell}\}) = \frac{X_j^{[m]}!}{(X_j^{[m]} - \sum_{\ell} \xi_{j\ell})! \prod_{\ell} \xi_{j\ell}!} \prod_{\ell} p_{j\ell}^{\xi_{j\ell}} \times \left(1 - \sum_{\ell} p_{j\ell}\right)^{(X_j^{[m]} - \sum_{\ell} \xi_{j\ell})}, \quad (1)$$

where $(X_j^{[m]} - \sum_{\ell} \xi_{j\ell})$ identifies the number of non traveling individuals, and we use standard numerical subroutines to generate random numbers of travellers following these distributions.

The transport operator in each city j is therefore written as

$$\Omega_j(\{X^{[m]}\}) = \sum_{\ell} (\xi_{\ell j}(X_{\ell}^{[m]}) - \xi_{j\ell}(X_j^{[m]})), \quad (2)$$

where the mean and variance of the stochastic variables are $\langle \xi_{j\ell}(X_j^{[m]}) \rangle = p_{j\ell} X_j^{[m]}$ and $\text{Var}(\xi_{j\ell}(X_j^{[m]})) = p_{j\ell}(1 - p_{j\ell}) X_j^{[m]}$. In addition, since the traffic flows are expressed as the number of available seats on a given connection, we have to consider that the transport operator is in general affected by fluctuations due to an occupancy rate of the airplanes not equal to 1. This introduces a further source of noise since we have to consider that on each connection (j, ℓ) the flux of passengers at each time t is given by a stochastic variable

$$\tilde{w}_{j\ell} = w_{j\ell}[\alpha + \eta(1 - \alpha)] \quad (3)$$

where $\alpha = 0.7$ corresponds to the average occupancy rate of 70% provided by official statistics [26] and η is a random number drawn uniformly in the interval $[-1, 1]$ at each time step.

Infection dynamics. The dynamics of the individuals $X^{[m]}$ between the different compartments depends on the specific disease considered. In compartmental models there are two possible elementary processes ruling the disease dynamics. The first class of process refers to the spontaneous transition of one individual from one compartment $[m]$ to another compartment $[h]$. Processes of this kind are the spontaneous recovery of infected individuals ($I \rightarrow R$) or the passage from a latent condition to an infectious one ($L \rightarrow I$) after the incubation period. In this

case the variation in the number of individuals $X^{[m]}$ is simply given by $\sum_h \nu_h^m a_h X^{[h]}$, where a_h is the rate of transition from the class $[h]$ and $\nu_h^m \in \{-1, 0, 1\}$ is the change in the number of $X^{[m]}$ due to the spontaneous process from or to the compartment $[h]$. The second class of processes refers to binary interaction among individuals such as the contagion of one susceptible in interaction with an infectious ($S + I \rightarrow 2I$). In the homogeneous assumption, the rate of variation of individuals $X^{[m]}$ is given by $\sum_{h,g} \nu_{h,g}^m a_{h,g} N^{-1} X^{[h]} X^{[g]}$, where $a_{h,g}$ is the rate of transition rate of the process and $\nu_{h,g}^m \in \{-1, 0, 1\}$ the change in the number of $X^{[m]}$ due to the interaction. The factor N^{-1} , where N is the number of individuals, stems from the fact that the above expression considers the homogeneous approximation in which the probability for each individual of class $[h]$ to interact with an individual of class $[g]$ is simply proportional to the density $X^{[g]}/N$ of such individuals (note that it is however possible to consider other cases [1]).

Stochastic formulation of the global spreading model. In order to go beyond the usual deterministic approximations, in each city we work directly with the master equations for the processes described above [23] and under the assumption of large populations we obtain the Langevin equations in which we associate to each reaction process a noise term with amplitude proportional to the square root of the reaction term [28, 29, 30]. The epidemic Langevin equations are coupled among them by the stochastic transport operator that describes movements of individuals from one city to another and can be numerically solved by considering the discretized evolution equations [28, 29, 30] for small time steps Δt that read

$$\begin{aligned}
X_j^{[m]}(t + \Delta t) - X_j^{[m]}(t) = & \sum_{h,g} N_j^{-1} \nu_{h,g}^m a_{h,g} X_j^{[h]}(t) X_j^{[g]}(t) \Delta t + \\
& + \sum_h \nu_h^m a_h X_j^{[h]}(t) \Delta t + \sum_{h,g} \nu_{h,g}^m \sqrt{a_{h,g} N_j^{-1} X_j^{[h]} X_j^{[g]}} \Delta t \eta_{h,g} + \\
& + \sum_h \nu_h^m \sqrt{a_h X_j^{[h]}} \Delta t \eta_h + \Omega_j(\{X^{[m]}\}), \tag{4}
\end{aligned}$$

where $\eta_{h,g}$ and η_h are statistically independent Gaussian random variables with zero mean and unit variance and $\Omega_j(\{X\})$ is the stochastic travel operator (defined in the previous paragraph)

depending on the traveling probabilities (obtained from the IATA dataset) $p_{j\ell} = w_{j\ell}\Delta t/N_j$. The model is thus a compartmental system of differential equations which can be numerically integrated. It is worth mentioning, however, that the standard integration of these equations by using Cauchy-Euler methods leads to a well-known technical problem and specific techniques must be used to avoid an asymmetric truncation of the noise terms [31].

The SIR dynamics.

Global epidemic forecast would be extremely relevant in the case of the emergence of a new pandemic influenza that in general spreads rapidly with substantial transmission occurring before the onset of case-defining symptoms. In the following we adopt a minimal model for a pandemic spread to provide a general discussion that is not hindered by the use of very complicated disease transmission mechanisms. Specific characteristics such as latency, incubation and seasonal effects of the disease can be however easily implemented in the present framework [17]. The analysis of two case studies and the comparison of the forecasts obtained with the present approach and the real data will be presented elsewhere. Here, we use the very simplistic approximation of the susceptible-infected-removed (SIR) dynamics in which a fully mixed population is assumed within each city. In each city j the population N_j is given by $N_j = S_j(t) + I_j(t) + R_j(t)$, where $S_j(t)$, $I_j(t)$ and $R_j(t)$ represent the number of susceptible, infected and recovered individuals at time t , respectively. The epidemic evolution is governed by the basic dynamical evolution of the SIR model where the probability that a susceptible individual acquires the infection from any given infected individual in the time interval dt is proportional to βdt , where β is the transmission parameter that captures the aetiology of the infection process. At the same time, infected individuals recover with a probability μdt , where μ^{-1} is the average duration of the infection. By considering the three compartments S , I and R in Eq.(4) and plugging in $a_{I,S} = \beta$, $a_I = a_R = \mu$ and the corresponding parameters $\nu_{I,S}^I = 1$ and $\nu_I^R = -\nu_I^I = 1$ it is possible to obtain explicitly the 3100×3 differential equations whose integration provides the disease evolution in every urban areas corresponding to an airport. Re-

sults shown in the following are obtained with the global spreading model based on an SIR dynamics within each city.

At first instance, it is possible to monitor standard epidemiological quantities such as the level of infected individuals, the morbidity and the prevalence at different granularity levels; i.e. country, state or administrative regions. In Fig. 2 we show the dynamical evolution in the US of an epidemic starting in Hong-Kong. The evolution of epidemic outbreaks is monitored by recording at each time step (1 day) the density of individuals in each class (S , I , R) present in each city. The parameters β and μ are chosen according to [21] in order to use biologically sound values and kept constant during the evolution (different values do not lead to different overall conclusions). This amounts to assume that no restrictions on traveling or targeted prophylaxis measures are implemented during the outbreak. We group the states in the nine influenza surveillance regions which are identical to the nine divisions of the US census and we use two different visualization strategies. In the first set of maps, regions are drawn with their normal size and a color code gives the prevalence of the infection in each region, i.e. the fraction of infected individuals. This representation readily shows the high heterogeneity of the pandemic evolution. While useful such a visualization might be misleading, since the same prevalence obtained in different regions might correspond to very different values in the number of infected individuals if the two regions are very differently populated. Moreover, it is common to find strong population density heterogeneities, and it is not easy to detect visually a large level of contamination in a small but densely populated geographical area. In order to obtain a geographical representation which is able to carry at the same time information both on the level of infection and on the infection cases in each region, we have constructed the corresponding cartograms of the original maps in which the size of each geographic region (in our case US influenza surveillance regions) is rescaled according to its population. Several methods for constructing cartograms have been developed (see [32] and references therein) and here we have adopted the diffusion-based method [32], which produces cartograms by equalizing the population density through a linear diffusion process. The geographical map representation

readily shows the heterogeneity of the spatio-temporal epidemic evolution but a quantitative characterization of this heterogeneity and its relation with the air transportation network statistical properties are major issues that are not yet fully explored.

Epidemic heterogeneity and network structure

In order to discriminate the role of the network structure on the spatio-temporal pattern of the epidemic process, we aim at a more quantitative analysis of its global heterogeneity. This heterogeneity might find its origin just in the stochastic nature of the infectious process or determined by the structural properties of the transportation network. In the latter case, it is possible to envision the possibility of a larger predictability of the epidemic behavior that would reflect the underlying network structure. Here we introduce for the first time a characterization of the epidemic pattern by using the entropy, a quantity customarily used in information theory to quantify the level of disorder of a signal or system. At each time step, a snapshot of the epidemic pattern is provided by the set of values of the prevalence $i_j(t) = I_j(t)/N_j$ in each city j . We can therefore define the normalized vector $\vec{\rho}$ with components $\rho_j = i_j / \sum_{\ell} i_{\ell}$ which contains the relevant information on the epidemic pattern. In particular, we can measure the level of heterogeneity of the disease prevalence by measuring the disorder encoded in the vector $\vec{\rho}$ with the normalized entropy function H

$$H(t) = -\frac{1}{\log V} \sum_j \rho_j(t) \log \rho_j(t). \quad (5)$$

If the epidemics is homogeneously affecting all nodes (i.e. all prevalences are equal) the entropy attains its maximum value $H = 1$. Starting from $H = 0$ which corresponds to one initial infected city - the most localized and heterogeneous situation - $H(t)$ increases as more cities become infected thus reducing the level of heterogeneity (see Fig. 3A). It is important to stress that in the present context the entropy does not have any thermodynamical meaning. It must be just considered as the appropriate mathematical tool able to quantify the statistical disorder of a complicate spatio-temporal signal.

To ascertain the effect of the network structure we compare the results obtained on the actual

network with those obtained on different network models providing null hypotheses (see Fig. 3). The first model network we consider (called *HOMN*) is a homogeneous Erdős-Rényi random graph with the same number of vertices V as the *WAN*, and is obtained as follows: for each pair of vertices (j, ℓ) , an edge is drawn independently, with uniform probability $p = \langle k \rangle / V$ where $\langle k \rangle$ is the average degree of the *WAN*. In this way, we obtain a typical instance of a random graph with a poissonian degree distribution, peaked around the average value $\langle k \rangle$ and decreasing faster than exponentially at large degree values, in strong contrast with the true degree distribution of the *WAN*. For the second model (called *HETN*) instead, we retain the exact topology of the real network. In both models, fluxes and populations are taken as uniform and equal to the corresponding averages in the actual air-transportation network.

The differences in the behavior observed in the *HOMN*, the *HETN* and in the real case provide striking evidence for a direct relation between the network structure and the epidemic pattern. The homogeneous network displays a homogeneous evolution (with $H \approx 1$) of the epidemics during a long time window, with sharp changes at the beginning and at the end of the spread. We observe a different scenario for heterogeneous networks where H is significantly smaller than one most of the time, with long tails signalling a long lasting heterogeneity of the epidemic behavior. Indeed, the analytical inspection of the epidemic equations points out that the broad variability of the contact pattern (degree distribution) and the ratios $w_{j\ell}/N_j$ play an important role in the heterogeneity of the spreading pattern. Strikingly, the curves obtained for both the real network and the *HETN* are similar, pointing out that in the case of the airport network the broad nature of the degree distribution determines to a large extent the overall properties of the epidemic pattern. Figure 3B reports the average entropy profile together with the maximal dispersion obtained for the spreading starting from a given city with different realizations of the noise. It is clear that the noise has a mild effect and that the average behavior of the entropy is representative of the behavior obtained in each realization. In Fig. 4 we show the percentage of infected cities as a function of time for each null model and for the real case. While the *HOMN* displays a long time window in which all cities are infected, this interval is

much smaller in the *HETN* and completely absent in the *WAN*.

Predictability and forecast reliability

A further major question in the modeling of global epidemics consists in providing adequate information on the reliability of the obtained epidemic forecast; i.e. the epidemic predictability. Indeed the intrinsic stochasticity of the epidemic spreading will make each realization unique and reasonable forecast can be obtained only if all epidemics outbreak realizations starting with the same initial conditions and subject to different noise realizations are reasonably similar. A convenient quantity to monitor in this respect is the vector $\vec{\pi}(t)$ whose components are $\pi_j(t) = I_j(t) / \sum_l I_l$; i.e the normalized probability that an infected individual is in city j . The similarity between two outbreaks realizations is quantitatively measured by the statistical similarity of two realizations of the global epidemic characterized by the vectors $\vec{\pi}^I$ and $\vec{\pi}^{II}$ respectively. As a measure of statistical similarity $sim(\vec{\pi}^I, \vec{\pi}^{II})$ we have considered the standard Hellinger affinity $sim(\vec{\pi}^I, \vec{\pi}^{II}) = \sum_j \sqrt{\pi_j^I \pi_j^{II}}$. Normalized similarity measures do not account for the difference in the total epidemic prevalence and we have to consider also $sim(\vec{i}^I, \vec{i}^{II})$ where $\vec{i}^{II} = (i^{II}, 1 - i^{II})$ and $i(t) = \sum_j I_j(t) / \mathcal{N}$ is the worldwide epidemic prevalence ($\mathcal{N} = \sum_j N_j$ is the total population). We can thus define the overlap function measuring the similarity between two different outbreak realizations as

$$\Theta(t) = sim(\vec{i}^I(t), \vec{i}^{II}(t)) \times sim(\vec{\pi}^I(t), \vec{\pi}^{II}(t)) \quad (6)$$

The overlap is maximal ($\Theta(t) = 1$) when the very same cities have the very same number of infectious individuals in both realizations, and $\Theta(t) = 0$ if the two realizations do not have any common infected cities at time t . Clearly, a large overlap corresponds to a predictable evolution, providing a direct measure of the reliability of the epidemic forecast. In the *HOMN* we find a significant overlap ($\Theta > 80\%$, see Fig. 5) even at the early stage of the epidemics - the most relevant phase for epidemic surveillance. The picture is different if we consider the *HETN* and the real airport network where especially at the initial stage of the epidemics the predictability is much smaller. These results may be rationalized by relating the level of predictability to the

presence of a backbone of dominant spreading channels defining specific “epidemic pathways” which are weakly affected by the stochastic noise. Epidemic pathways are the outcome of the conflict between two different properties of the network. On the one hand, the heterogeneity of the connectivity pattern provides a multiplicity of equivalent channels for the travel of infected individuals depressing the predictability of the evolution. On the other hand, the heterogeneity of traffic flows introduces dominant connections which select preferential pathways increasing the epidemic predictability. The heterogeneous connectivity pattern of the *HETN* and the *WAN* thus generates a multiplicity of channels that decreases the predictability. In the real case the lowering of the epidemic predictability also indicates the dominant effect of the topological heterogeneity that wins over the opposite tendency of the traffic heterogeneity. The above framework is confirmed by the two distinct behaviors depending on the degree of the initial infected city. Epidemics starting in initial cities with a hub airport generate realizations whose overlap initially decreases to 50-60% because of the many possible equivalent paths resulting in a larger differentiation of the epidemic history in each stochastic realization. On the contrary, outbreaks from poorly connected initial cities display a large overlap due to the few available connections that favor the selection of specific epidemic pathways.

Outlook

From our study, it emerges that the air transportation network properties are responsible of the global pattern of emerging diseases. In this perspective, the complex features characterizing this network are the origin of the heterogeneous and seemingly erratic spreading on the global scale of diseases such as SARS. The analysis provided here show that large scale mathematical models that takes fully into account the complexity of the transportation matrix can be used to obtain detailed forecast of emergent disease outbreaks. We have also shown that it is possible to provide quantitative measurements of the predictability of epidemic patterns, providing a tool that might be used to obtain confidence intervals in epidemic forecast and in the risk analysis of containment scenarios. It is clear that to make the forecast more realistic, it is necessary to

introduce more details in the disease dynamics. In particular, seasonal effects and geographical heterogeneity in the basic transmission rate (due to different hygienic conditions and health care systems in different countries) should be addressed. Finally, the interrelation of the air transportation network with other transportation systems such as railways and highways could be very useful for forecast on longer time scales. We believe however that the basic understanding of the interplay of the transportation network complex features with the disease spreading evolution and the detailed modeling obtained by the full consideration of these features may represent a valuable tool to test traveling restrictions and vaccination policies in the case of new pandemic events.

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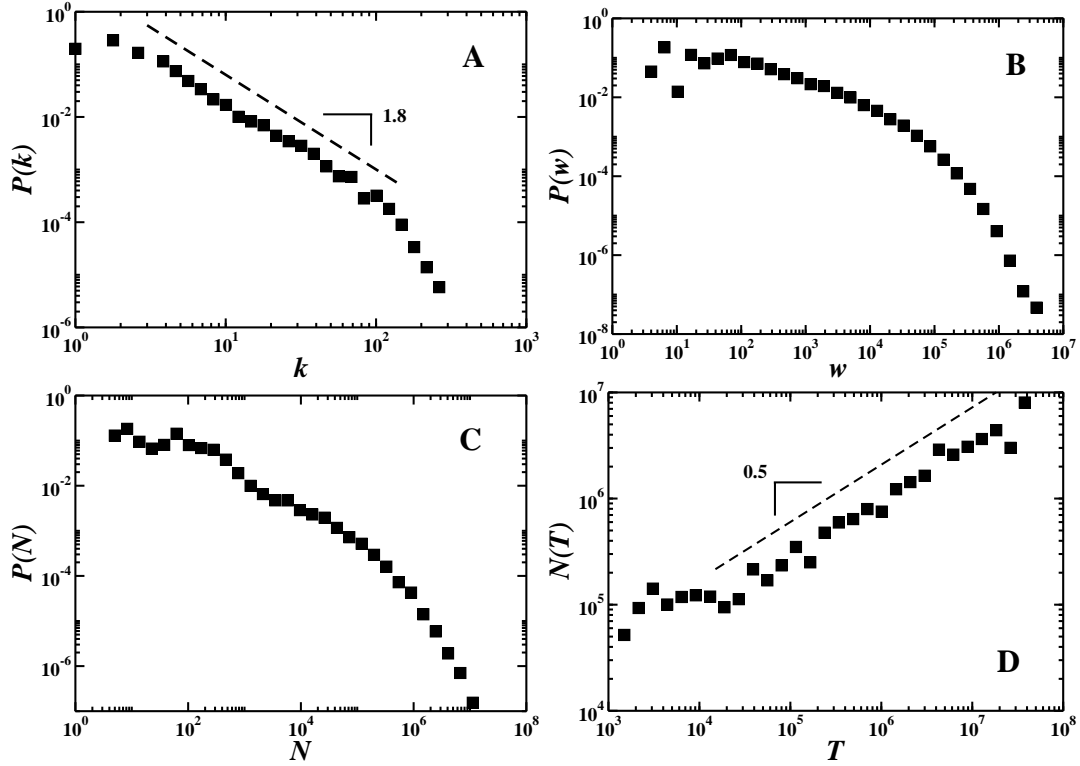


Figure 1: Properties of the world-wide airport network. Statistical fluctuations are observed over a broad range of length scales. **(A)** The degree distribution $P(k)$ follows a power-law behavior on almost two decades with exponent 1.8 ± 0.2 . **(B)** The distribution of the weights (fluxes) is skewed and heavy-tailed. **(C)** The distribution of populations is heavy-tailed distributed, in agreement with the commonly observed Zipf's law [27]. **(D)** The city population varies with the traffic of the corresponding airport as $N \sim T^\alpha$ with $\alpha \simeq 0.5$, in contrast with the linear behavior postulated in previous works [23].

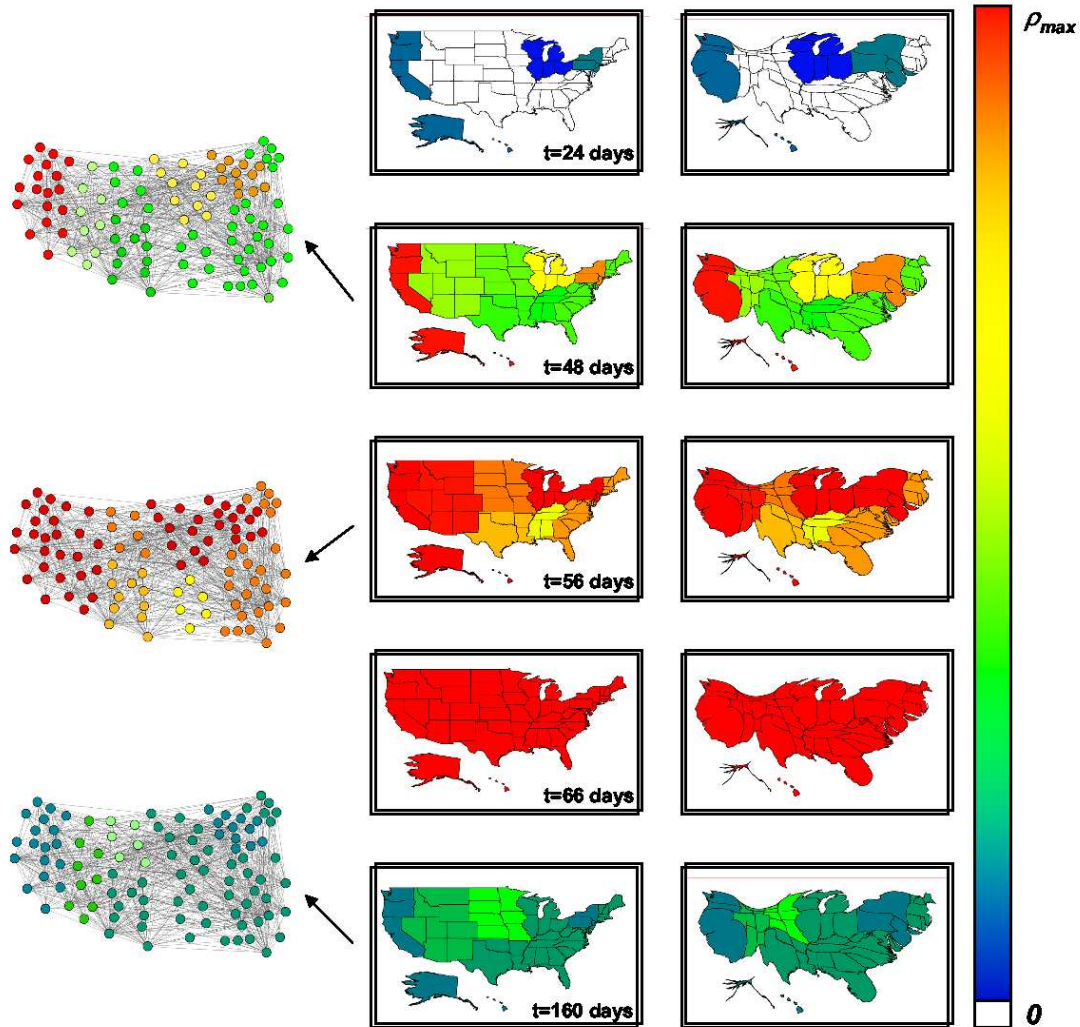


Figure 2: Geographical representation of the disease evolution in the US for an epidemics starting in Hong Kong based on an SIR dynamics within each city. States are collected according to the nine influenza surveillance regions. The color code corresponds to the prevalence in each region, from 0 to the maximum value reached (ρ_{max}). On the left the original US maps are shown, while on the right we provide the corresponding cartograms obtained by rescaling each region according to its population. Three representations of the airport network restricted to the US are also shown, in correspondance to three different snapshots. The nodes represent the 100 airports in the US with highest traffic T ; the color is assigned in accordance to the color code adopted for the maps.

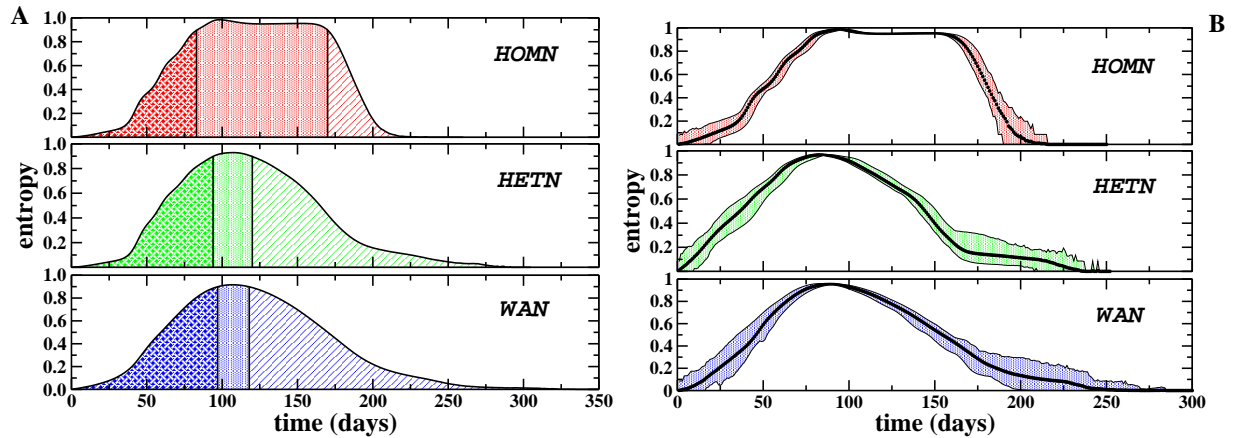


Figure 3: Analysis of the heterogeneity of the epidemic pattern in the actual network (*WAN*) compared with the two network models (*HOMN*) and (*HETN*). An SIR dynamics is adopted within each city. **(A)** Entropy $H(t)$ averaged over distinct initial infected cities and over noise realizations. Each profile is divided into three different phases, the central one corresponding to $H > 0.9$, i.e. to a homogeneous geographical spread of the disease. This phase is much longer for the *HOMN* than for the real airport network. The behavior observed in *HETN* is close to the real case meaning that the connectivity pattern plays a leading role in the epidemic behavior. **(B)** Average value of the entropy, with the maximal dispersion obtained from $2 \cdot 10^2$ noise realizations of an epidemics starting in Hong Kong. Fluctuations have a mild effect in all cases.

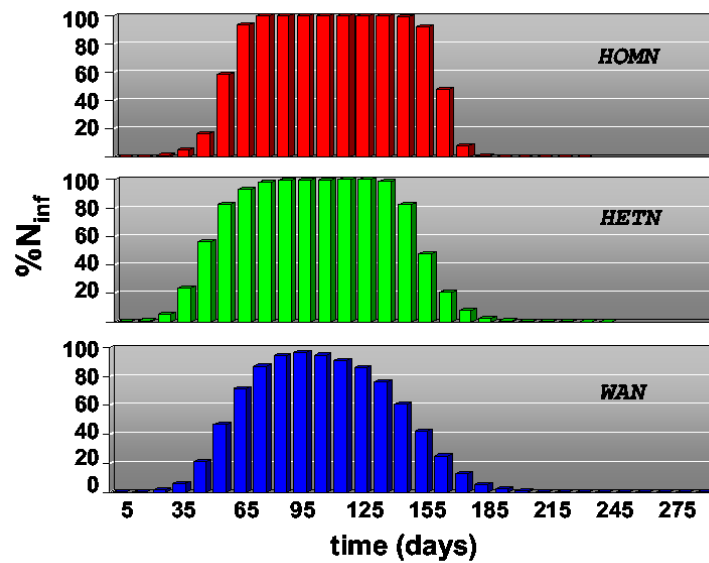


Figure 4: Percentage of infected cities as a function of time for an epidemics starting in Hong Kong based on an SIR dynamics within each city. The *HOMN* case displays a large interval in which all cities are infected. The *HETN* and the real case show a smoother profile with long tails, signature of a long lasting geographical heterogeneity of the epidemic diffusion.

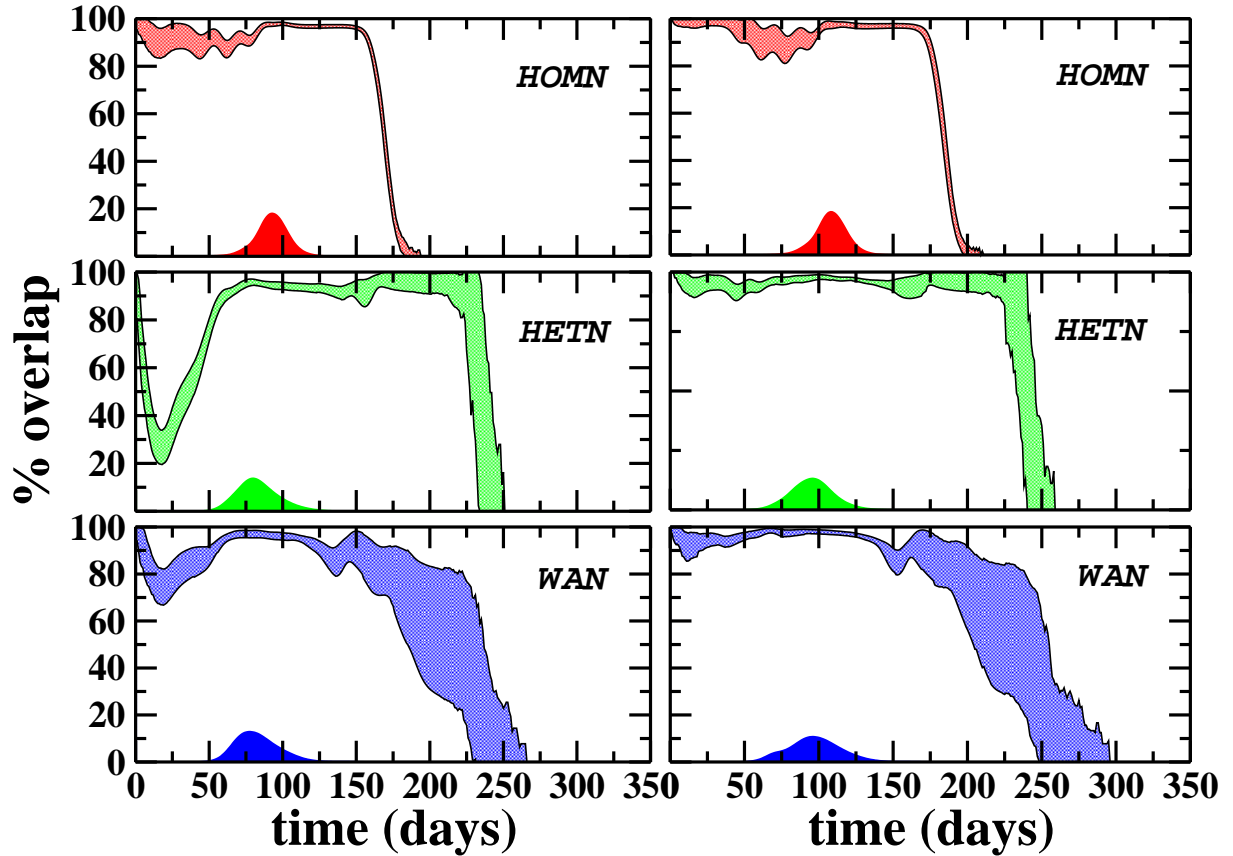


Figure 5: Percentage of overlap as a function of time: the shaded area corresponds to the standard deviation obtained with $5 \cdot 10^3$ couples of different realizations of the global spreading model based on an SIR dynamics within each city. Topological heterogeneity plays a dominant role in reducing the overlap in the early stage of the epidemics. We observe two different behaviors depending on the degree of the initially infected city: a reduced initial predictability in the case of airport hubs (left) with respect to poorly connected cities (right). Large fluctuations at the end of the epidemics are observed in the *HETN* and in the real case, due to the different lifetime of the epidemics in distinct realizations induced by the heterogeneity of the network. We also report the prevalence profile as a function of time showing that the maximum predictability corresponds to a prevalence peak.